## The QCD phase transition(s) from model to observable

Jan Steinheimer

09/20/2016



## The new/current pig in town

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Let's focus on the current pig(s) in town

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Both are rather "difficult" regarding modeling. Fluctuations amplify the signal, but also uncertainties. Why dynamical models?

- Finite number of particles and volume
- Conservation laws
- Finite Lifetime
- Can separate out different physics effects

...

# Equilibrium Phase Transition (Maxwell construction)

As the system dilutes, the phases are always well separated



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#### Non-Equilibrium Phase Transition

Phase separation is a dynamical process.







## Phase separation

Initialize Random noise in the unstable region and let the phases separate.



Requires: Fluid dynamics  $+ \mbox{ an EoS}$  with mechanically unstable phase + the surface energy

## Can be done, has been done

Initialize Random noise in the unstable region and let the phases separate.

Ideal fluid dynamics + an EoS with mechanically unstable phase + the surface energy

## Moments of the Baryon Density

Extract moments of the net baryon density distribution:

$$\langle 
ho^N 
angle ~\equiv~ rac{1}{A} \int 
ho(m{r})^N 
ho(\mathbf{r}) \, d^3m{r}$$



#### Usually one measures moments of Number-distributions

- Variance  $\sigma^2 = \left< \delta N^2 \right>$
- Skewness  $S = \left< \delta N^3 \right> / (\sigma^2)^{3/2}$
- Kurtosis  $\kappa = (\left< \delta N^4 \right> / \sigma^4) 3$

Can also be extracted from fluid dynamics, in a spatial volume.

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- Fluctuation on all possible scales
- No creation of fluctuations by the EoS. Driven by field dynamics/ thermal fluctuations.

## The Critical Point



Can be done:

- Fluid dynamics
- + The correct EoS
- + thermal fluctuations / explicit propagation of chiral field
- = chiral fluid dynamics

M.Nahrgang, S.Leupold, C.Herold and M.Bleicher, Phys. Rev. C **84, 024912 (2011)** 

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- Cooper-Frye, the big poissonizer
- Effects of the final/hadronic phase.
- Measuring deuterons?

### What are volume fluctuations?

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- Emission of particles does not occur at a fixed time.
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- Usually (an average)  $N_{part}$  is taken as proxy for the volume. Or better the energy content of the system.

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- Use Cooper-Frye for particle production
- $\bullet\,$  Then calculate the net baryon number  $\sigma/M$  in a given longitudinal interval

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- Interesting z-dependence.
- Problem: N<sub>part</sub> definition in models ≠ definition in experiment.

#### Stopping in transport

- For beam energies  $> \sqrt{s_{\rm NN}} \approx 7 \text{ GeV} \rightarrow \text{string excitation}.$
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- Strong correlation between rapidity and z-coordinate.
- Stopping in A+A due to secondary interactions.

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#### Stopping in transport

- Question 1: How well are the secondaries understood?
- Question 2: What if there is no instant energy loss?



A. Bialas, A. Bzdak and V. Koch, arXiv:1608.07041 [hep-ph].

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Energy loss is more complicated.

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#### Stopping in transport

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May be relevant for  $v_1$  too!?

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M. Hempel, V. Dexheimer, S. Schramm and I. Iosilevskiy, Phys. Rev. C 88, no. 1, 014906 (2013)

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- One cannot separate small  $\mu_B$  and large  $\mu_B$  regions.
- Standard quark based models usually fail this test.

#### A hadronic part

The parity doublet model: nucleons (hyperons) and their parity partners belong to the same multiplet and so are true chiral partners.

+

#### A quark+gluon part

Use a simple version of the PNJL model

+

#### A way to suppress hadrons in the QGP

Use excluded volume

#### An effective Q-H model

Work in progress: A. Mukherjee, JS and S. Schramm



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- Good description of the hadronic high density sector
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- What is the interplay between the nuclear L-G transition and the chiral transition?
- Pressure vs. Temperature along transition lines.
- High density: Intermingling between both transitions.



#### Normalized cumulants as function of T and $\mu_B$ .





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• The nuclear L-G effects are relevant also at larger temperatures!





- The nuclear L-G effects are relevant also at larger temperatures!
- A study of the cumulants should never neglect the role of both transitions

• When do the fluctuations freeze out?



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- Beam energy dependence along different freeze out lines.



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Of course another freeze out scenario is also possible.

### Whats with the banana shape?

- An idea was put forward that the normalized cumulants as function of each other give a characteristic shape.
- In the presence of two transitions the picture becomes more complicated.



# The (Non-)Strange EoS

 At the beam energies of SIS100/FAIR/BESII strangeness is severely suppressed/ out-of-equilibrium.



A. Andronic et al., Nucl. Phys. A 772, 167 (2006)

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- At the beam energies of SIS100/FAIR/BESII strangeness is severely suppressed/ out-of-equilibrium.
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- Think about strangeness distillation and iso.spin distillation.



J.S. and M. Bleicher, Phys. Rev. C 84, 024905 (2011)

# Cooper-Frye, the big Poissonizer

How is Cooper-Frye used

$$E\frac{dN}{d^3p} = \int_{\sigma} f(x,p) p^{\mu} d\sigma_{\mu}$$

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- Does C.-F. reproduce the moments in coordinate space?

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- We employ the standard C-F procedure, conserving baryon number globally.





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- Instead of cutting in coordinate space, cutting in momentum space
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- Raises the question whether one should use C-F for particle production in studies related to fluctuations.
- Can we come up with a better scheme?
- An event generator that reproduced the desired moments.

The hadronic rescattering J. Steinheimer, V. Vovchenko, J. Aichelin, M. Bleicher and H. Stöcker. arXiv:1608.03737 [nucl-th].

- The density just after hadronization is still large enough for sufficient rescatterings to take place.
- kinetic freeze out  $\neq$  latest point of chemical equilibrium.



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- kinetic freeze out  $\neq$  latest point of chemical equilibrium.
- Mainly (pseudo-)elastic scattering and resonance excitations.



#### The hadronic rescattering

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$$r_{\rm IF}(t) = \frac{\sum_{n} (I_n(t) - \overline{I}(t))(F_n - \overline{F})}{\sqrt{\sum_{n} (I_n(t) - \overline{I}(t))^2 \sum_{n} (F_n - \overline{F})^2}}$$



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#### The hadronic rescattering

Beam energy dependence almost flat



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- Beam energy dependence almost flat
- Smearing is considerable



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- Survival time of different orders of cumulants?
- Need for non-Poisson event generator.

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Simple coalescence picture

$$\lambda_d = Bn_p \cdot n_n$$

The deuteron yield  $n_d$  in an event with initial proton multiplicity  $n_i$  then fluctuates according to a Poisson distribution

$$P_d(n_d|n_i) = \lambda_d^{n_d} \frac{e^{-\lambda_d}}{n_d!} = (Bn_i^2)^{n_d} \frac{e^{-Bn_i^2}}{n_d!}$$

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- Essentially like an efficiency, but multiplicity dependent.
- Results depends on how much proton and neutron number is correlated.



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Is it worth the effort?