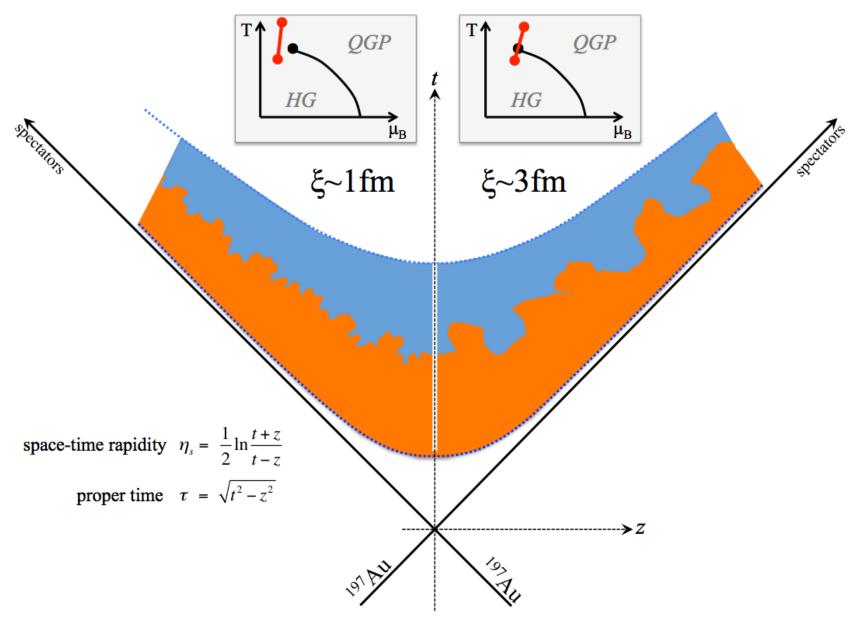
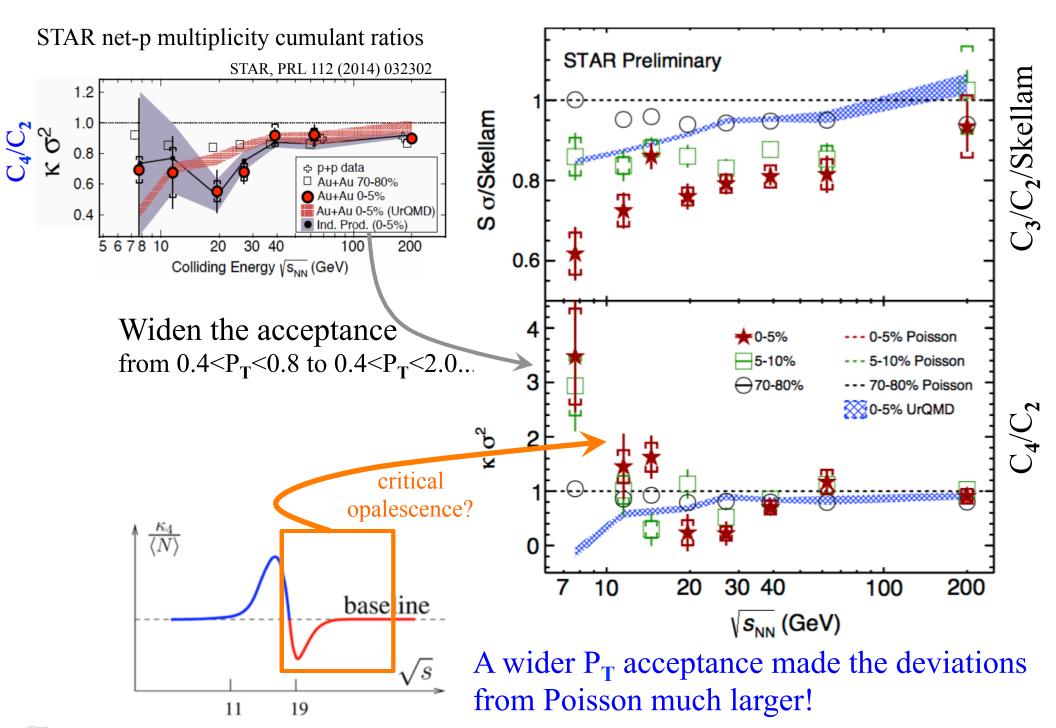
Rapidity Correlations

W.J. Llope for the STAR Collaboration Wayne State University









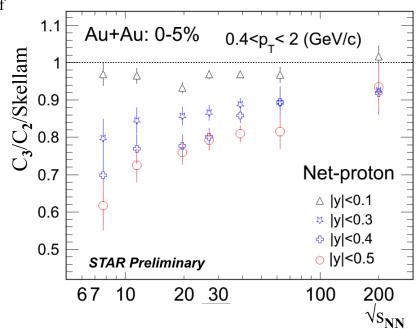
In a small acceptance, you will see Poissonian cumulant ratios, CP or not....

V. Koch, RIKEN BNL Research Center Workshop on Fluctuations, Correlations and RHIC Low Energy Runs, October 3-5, 2011

http://quark.phy.bnl.gov/~htding/fcrworkshop/Koch.pdf

decreasing rapidity acceptance in the analysis also drives the C_4/C_2 values to Poisson:

see also D. Mahapatra *et al.*, arXiv nucl-ex/0108011v2



Net-baryon Acceptance:





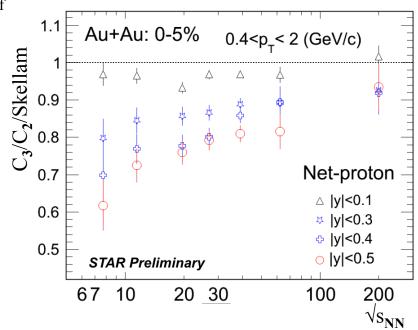
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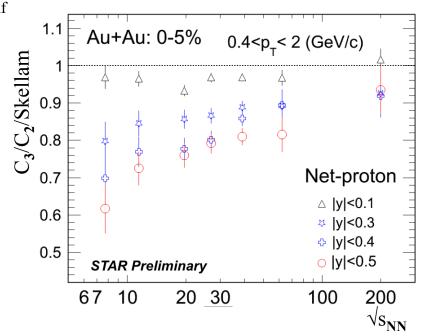
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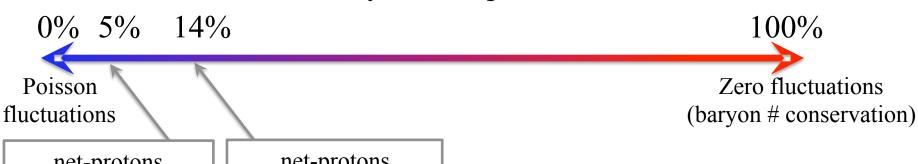
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Net-baryon Acceptance:



net-protons $0.4 < P_T < 0.8$, |y| < 0.5 $C_1 \sim 8$ @ 19.6GeV net-protons $0.4 < P_T < 2.0, |y| < 0.5$ $C_1 \sim 22 @ 19.6 GeV$

Let's look differentially in rapidity.

$$R_2 = \frac{C_2(y_1, y_2)}{\rho_1(y_1)\rho_1(y_2)} = \frac{\rho_2(y_1, y_2)}{\rho_1(y_1)\rho_1(y_2)} - 1$$

same event mixed events or tensor product of 1D

lead to "cluster" picture...

- clusters decay to FS particles
- clusters uncorrelated w/ each other
- isotropic decay of clusters in their rest frames
- Lorentz-invariant translation of clusters in pseudorapidity

Exposes short and long-range correlations:

E & p conservation minijets HBT, Bose-Einstein, *etc*.

L. Foà, Phys. Lett. C22, 1 (1975)H. Bøggild, Ann. Rev. Nucl. Sci. 24, 451 (1974)M. Jacob, Phys. Rep. 315, 7 (1999)

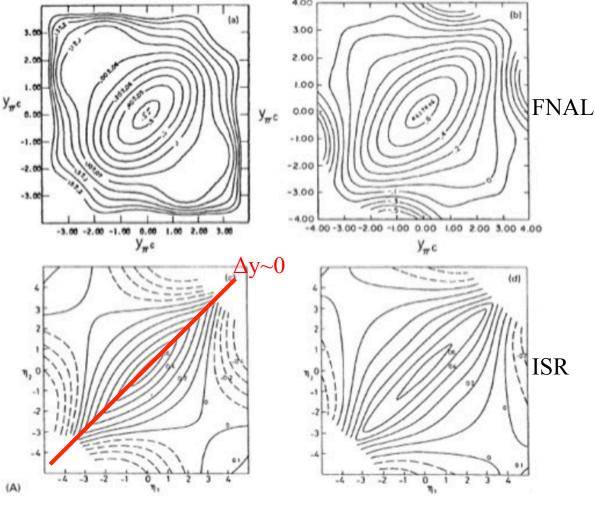


Figure 3.5: R_2^{cc} for p+p collisions at FNAL (a-b)and CERN ISR (c-d): $\sqrt{s}=13.7$, 27, 23, 63 GeV.



Recall how fourier decomposition of azimuthal angle distrubutions leads to all sorts of interesting information on elliptic flow, flow fluctuations, triangularity....

A similar approach can be applied to study the shape of the fireball in the longitudinal direction!

Long-range rapidity correlations as fluctuating rapidity density of the fireball:

A. Bialas, A. Bzdak, and K. Zalewski, Phys. Lett. B 710, 332 (2012).

A. Bialas and K. Zalewski, Acta Phys. Pol. B 43, 1357 (2012).

...possibly with a significant asymmetric component in fireball's rapidity shape:

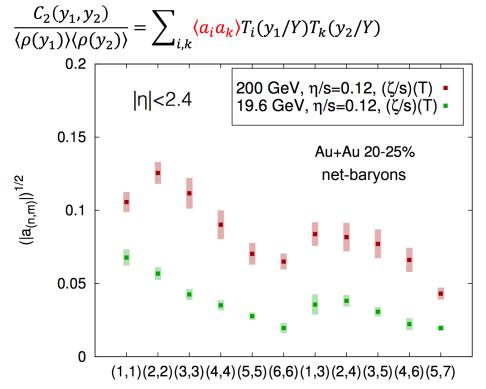
B. I. Abelev et al. (STAR Collaboration), Phys. Rev. Lett. 103, 172301 (2009).

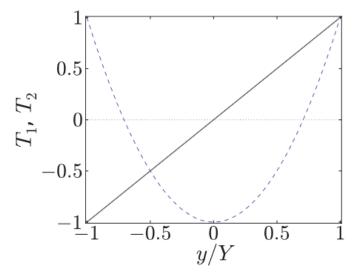
...Generalize!

A. Bzdak and D. Teaney, Phys. Rev. C 87, 024906 (2013)

$$C(y_1, y_2) \equiv \rho_2(y_1, y_2) - \rho(y_1)\rho(y_2)$$

...decompose rapidity cumulant into Chebyshev polynomials...





information on the number of sources, baryon stopping mechanisms, viscosity, ...

See also:

A. Bzdak, Phys. Rev. C 85, 051901(R) (2012)

T. Lappi & L. McLerran, Nucl. Phys. A 832, 330 (2010)

A. Monnai, B. Schenke, arXiv:1509.04103

A. Bzdak (QM2015) 29/9/2015 16:00-16:20

B. Schenke (QM2015) 30/9/2015 9:20-09:40



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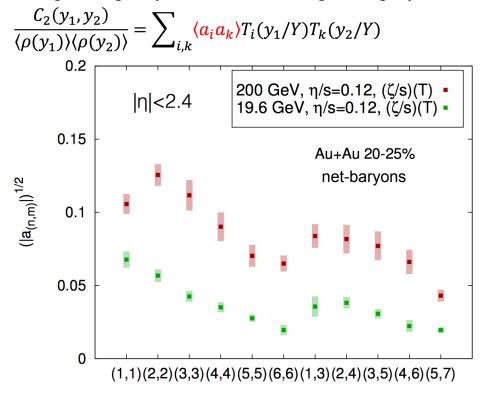
B. I. Abelev et al. (STAR Collaboration), Phys. Rev. Lett. 103, 172301 (2009).

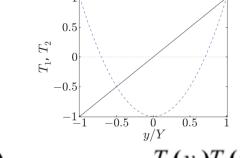
...Generalize!

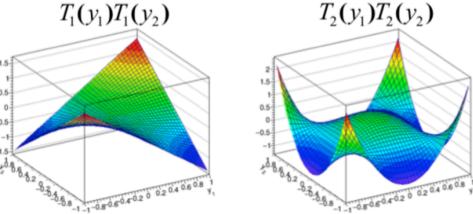
A. Bzdak and D. Teaney, Phys. Rev. C 87, 024906 (2013)

$$C(y_1, y_2) \equiv \rho_2(y_1, y_2) - \rho(y_1)\rho(y_2)$$

...decompose rapidity cumulant into Legendre polynomials...







information on the number of sources, baryon stopping mechanisms, viscosity, ...

See also:

A. Bzdak, Phys. Rev. C 85, 051901(R) (2012)

T. Lappi & L. McLerran, Nucl. Phys. A 832, 330 (2010)

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Recently, this variable has reappeared with a new name: $C(y_1, y_2) \dots C(y_1, y_2) = R_2(y_1, y_2) + 1$

$$R_2 = \frac{C_2(y_1, y_2)}{\rho_1(y_1)\rho_1(y_2)} = \frac{\rho_2(y_1, y_2)}{\rho_1(y_1)\rho_1(y_2)} - 1$$



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$$C(y_1, y_2) = 1 + \frac{1}{2} < a_0 a_0 > + \frac{1}{\sqrt{2}} \sum_{n=1}^{\infty} < a_0 a_n > (T_n(y_1) + T_n(y_2)) + \sum_{n,m=1}^{\infty} < a_n a_m > \frac{T_n(y_1) T_m(y_2) + T_n(y_2) T_m(y_1)}{2}$$

J. Jia, S. Radhakrishnan, and M. Zhou, Phys. Rev. C93, 044905 (2016), arXiv:1506.03496



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reflects the multiplicity fluctuations in the event



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reflects the multiplicity represents residual centrality

fluctuations in the event dependence in the shape of $\langle N(y) \rangle$

With a special normalization, the residual centrality dependence is largely eliminated.

$$C_N(y_1, y_2) = \frac{C(y_1, y_2)}{C_p(y_1)C_p(y_2)}$$

$$C_p(y_1) = \frac{\int_{-Y}^{Y} C(y_1, y_2) dy_2}{2Y}, C_p(y_2) = \frac{\int_{-Y}^{Y} C(y_1, y_2) dy_1}{2Y}$$

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fluctuations in the event dependence in the shape of $\langle N(y) \rangle$

encodes the dynamical shape fluctuations for events with the same centrality

With a special normalization, the residual centrality dependence is largely eliminated.

$$C_{N}(y_{1}, y_{2}) = \frac{C(y_{1}, y_{2})}{C_{p}(y_{1})C_{p}(y_{2})}$$

$$C_{p}(y_{1}) = \frac{\int_{-Y}^{Y} C(y_{1}, y_{2}) dy_{2}}{2Y}, C_{p}(y_{2}) = \frac{\int_{-Y}^{Y} C(y_{1}, y_{2}) dy_{1}}{2Y}$$

$$C_{N}(y_{1}, y_{2}) = 1 + \sum_{n,m=1}^{\infty} \langle a_{n} a_{m} \rangle \frac{T_{n}(y_{1})T_{m}(y_{2}) + T_{n}(y_{2})T_{m}(y_{1})}{2}$$

$$\frac{T_{1}(y_{1})T_{1}(y_{2})}{a_{n} a_{n} a_{n} a_{n}} = \frac{T_{1}(y_{1})T_{2}(y_{2})}{2Y}$$

$$T_{2}(y_{1}, y_{2}) = 1 + \sum_{n,m=1}^{\infty} \langle a_{n} a_{m} \rangle \frac{T_{n}(y_{1})T_{m}(y_{2}) + T_{n}(y_{2})T_{m}(y_{1})}{2}$$

Dynamical shape fluctuations (and correlations) can be quantified by decomposing the measured distributions onto a basis set of Legendre polynomials, with "strength" coefficients <a_ma_n>

Rapidity analog of decomposition of azimuthal anistropies onto $\cos(n\phi...)$ bases with strengths v_n



Datasets: All 8 BES energies

POI: $h\pm$, $K\pm$, & $p\pm$

2σ on dE/dx, then require good TOF m²

General cuts: |Zvtx| < 30cm at all $\sqrt{s_{NN}}$

Nhitsfit>15 gDCA<2cm

 p_{T}^{min} : 0.2 for h± & K±, 0.4 for p±

 p_T^{max} : 2.0

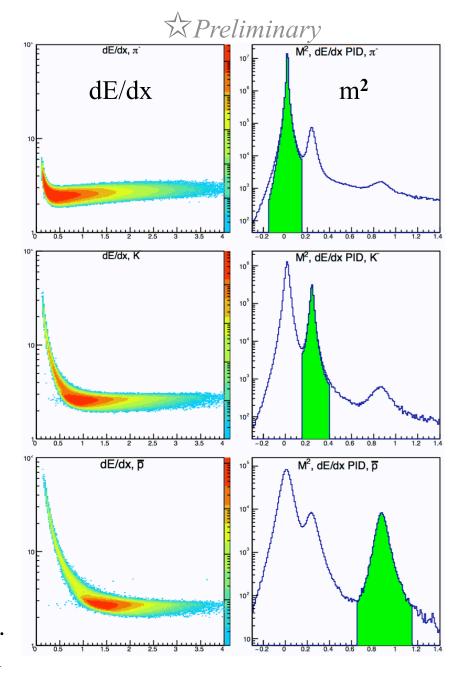
 p^{max} : 1.6 for $h \pm \& K \pm$, 3.0 for $p \pm$

Centrality: N_{tracks} with 0.5< η <1 for h± & K±

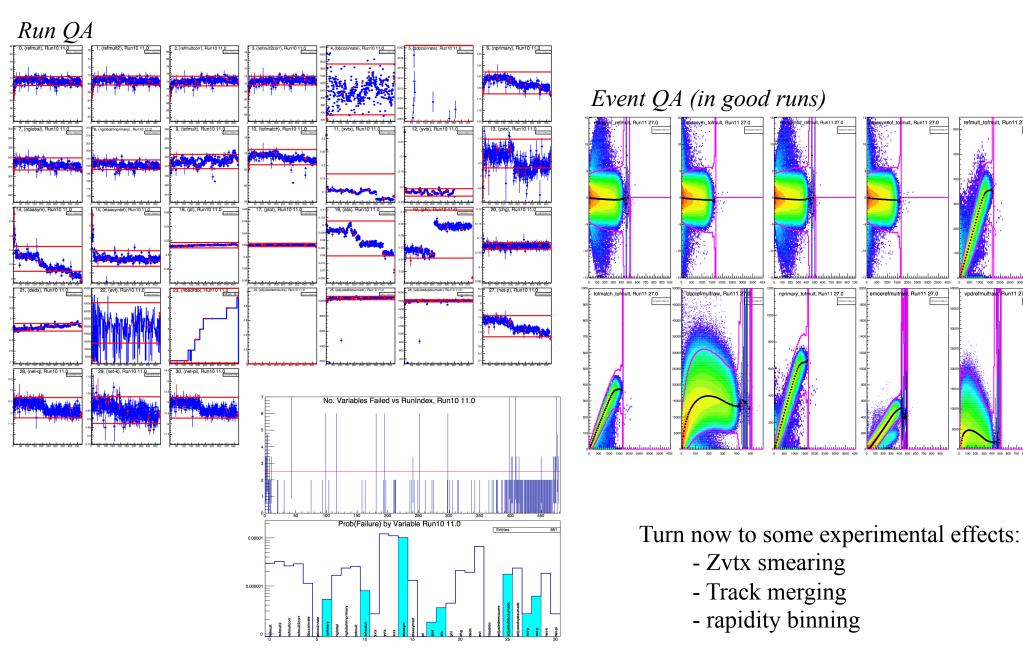
 $N_{\pi,K}$ with 0.5< η <1 for p±

Cuts & centrality intentionally very close to those used in recent \Leftrightarrow multiplicity cumulant analyses.

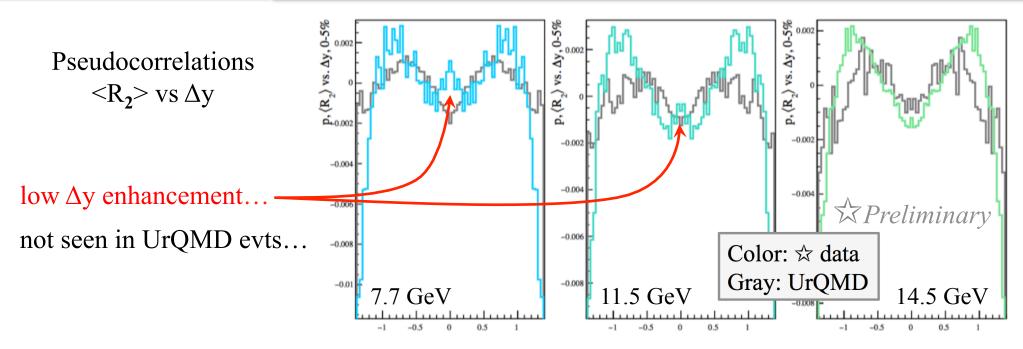
Same analysis code used for UrQMD events ~20M min. bias events available at each $\sqrt{s_{NN}}$... Parameterized exp. efficiency vs (PID,pt,y,cent)... Centrality via cuts on b when integrated w/ RM>1



Careful good run & good event QA performed...

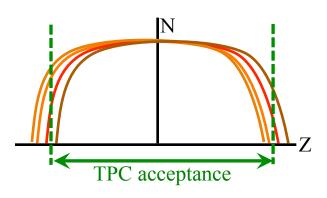




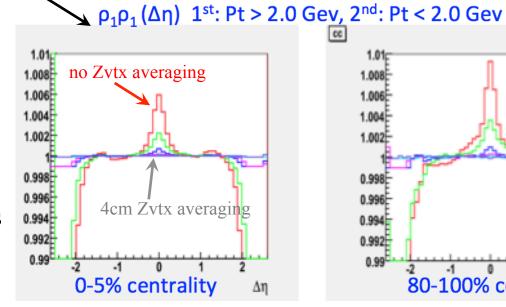


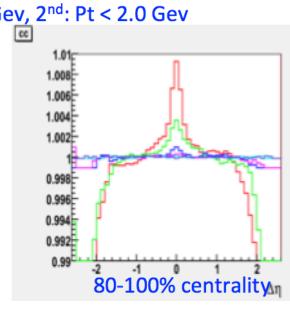
Caused by rapidity dependence of experimental efficiency coupled with Zvtx smearing...

See L. Tarini, Ph.D. Thesis, and his talk at the STAR Analysis Meeting, MIT, 7/10/2009



Now I analyze in 2cm-wide Zvtx bins then weight-average the results...



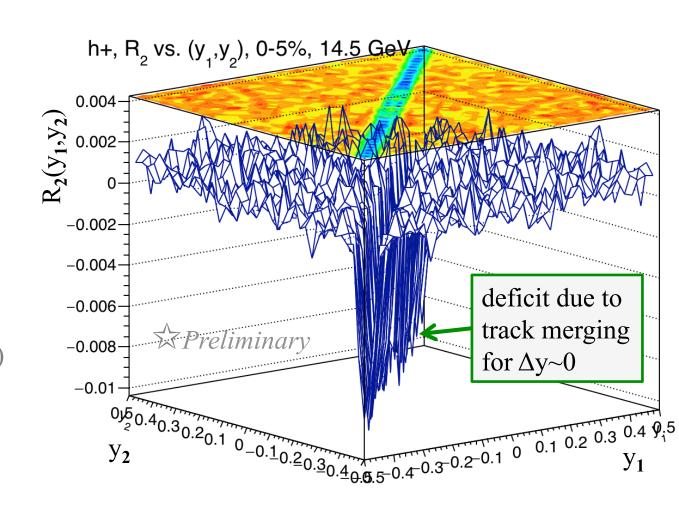


Very strong trench in R_2 when particle multiplicities/event of POI get large: $h\pm$ for all centralities and $\sqrt{s_{NN}}$, and only most central for $K\pm$

Numerator and denominator of R_2 & C_N uses only measured tracks... but there is a slight 2-particle efficiency loss when two tracks are nearby ($\Delta y \sim 0$)

The STAR track-finder "sti" does not share spacepoints!

a new one does "stiCA" (10%)





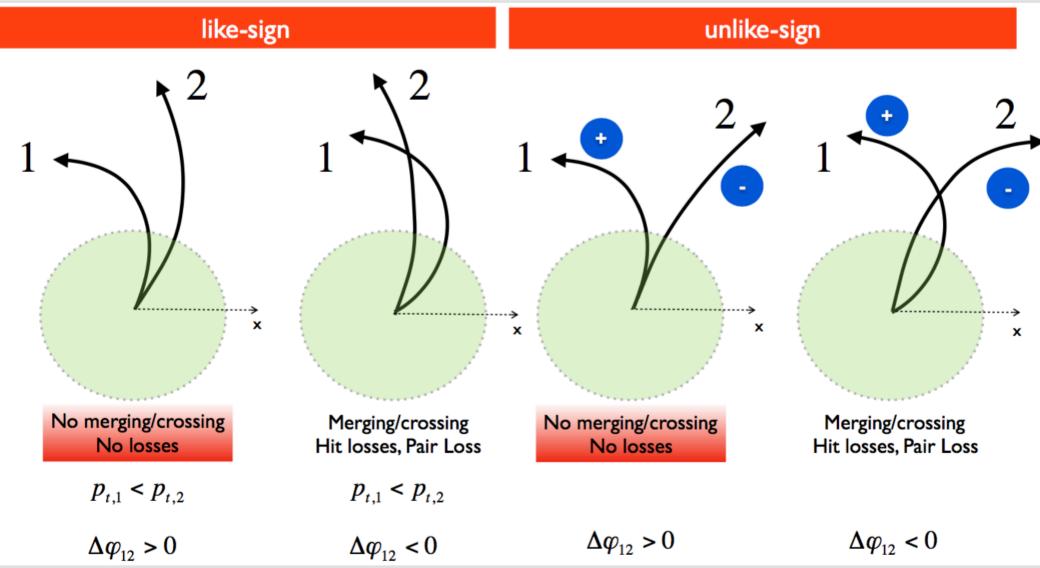


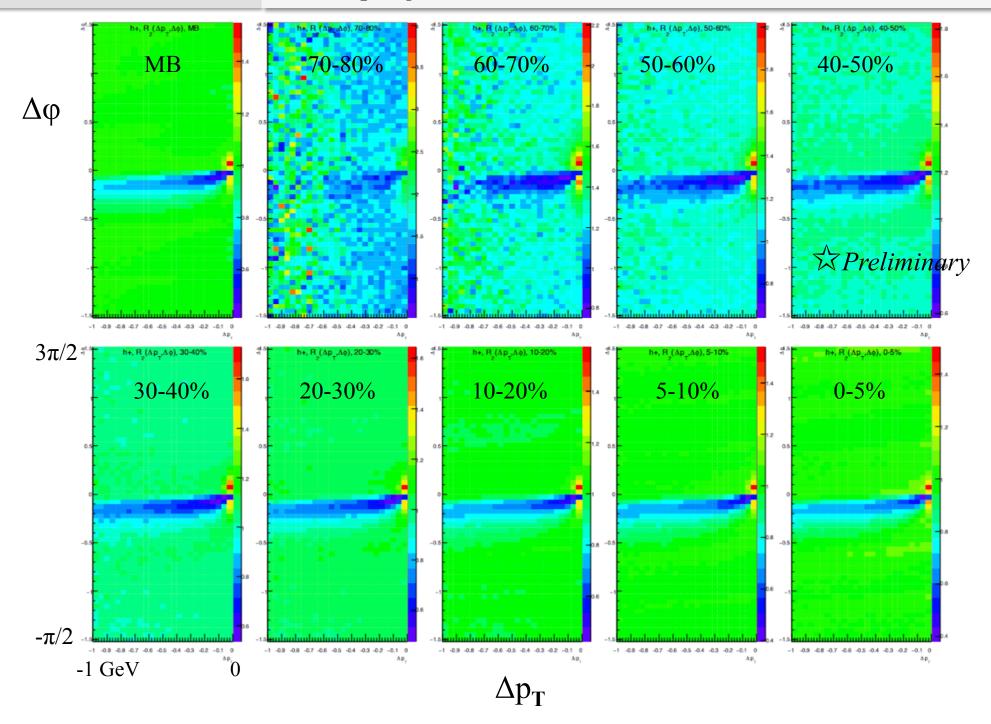
Image from P. Pujahari

LS & US: reflect clean area in $\Delta \varphi$ to replace problem area

US: nothing special in fill method

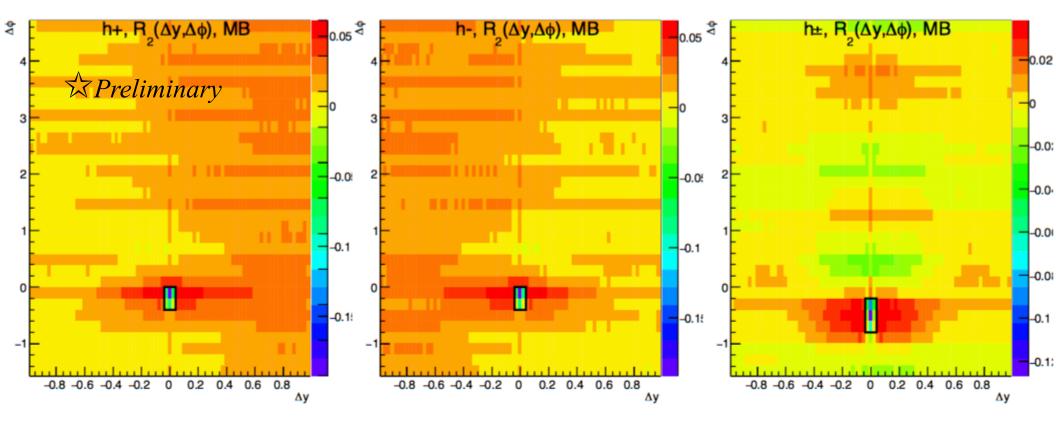
LS: pT order the tracks, fill numerator for upper triangle only, then symmetrize







unsymmetrized $R_2(\Delta y, \Delta \phi)$



Thus cannot simply start from $\rho_2(y_1,y_2)$ and $\rho_1(y_1)*\rho_1(y_2)...$

...I must calculate each as 3D hists as $(y_1, y_2, \Delta \varphi)$

Several symmetrization approaches tried to "fill" merging hole... All tricky

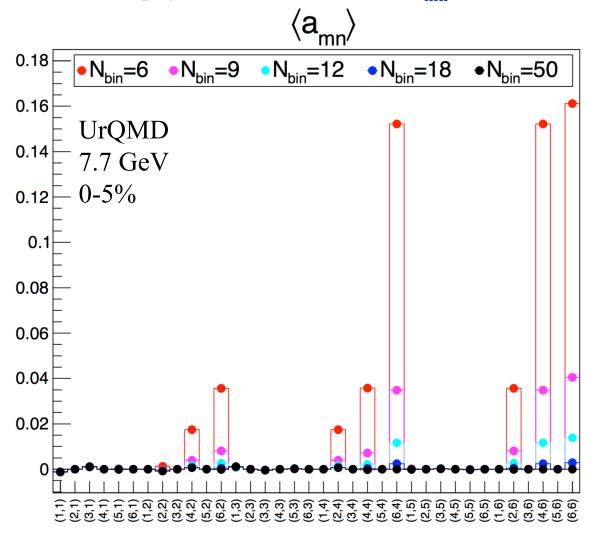
For now, just cut out the merging hole in both same and mixed event histograms

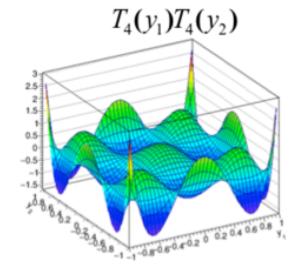


The cut used is $|\Delta y| < 0.04$ and $-5\pi/12 \le \Delta \phi < 0$

Given this cut, I cannot bin the (y1,y2) parts of the TH3D too finely! (or there will never be any counts in the $\Delta y=0$ bins) Rapidity bin width must be near or larger than 2*0.04...

But this can cause non-physical artifacts in the $\langle a_{mn} \rangle$ values!

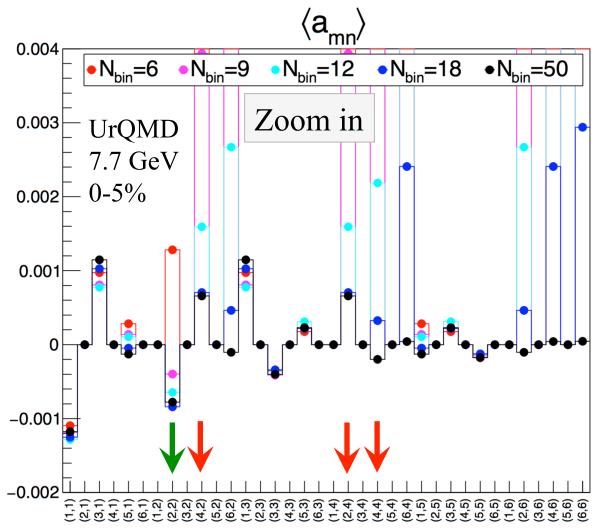


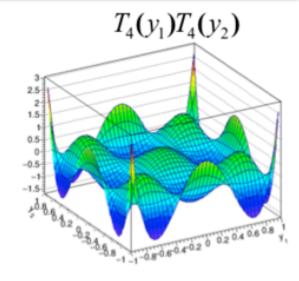


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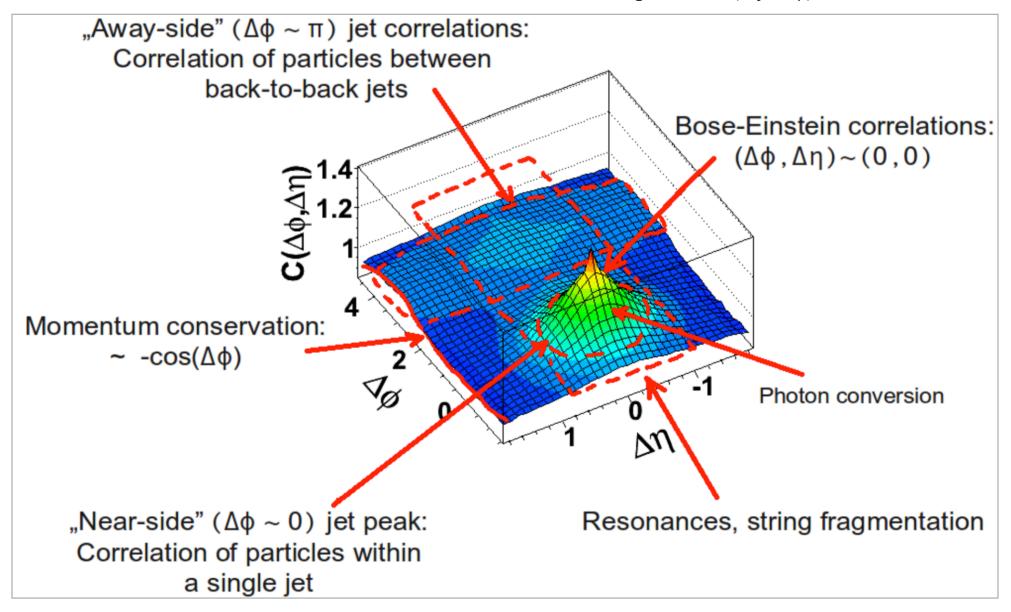




-0.72<y<0.72 (2,2) stable for $N_{bin} \ge 12$ (2,4) stable for $N_{bin} \ge 18$ (4,4) stable for $N_{bin} >> 18$

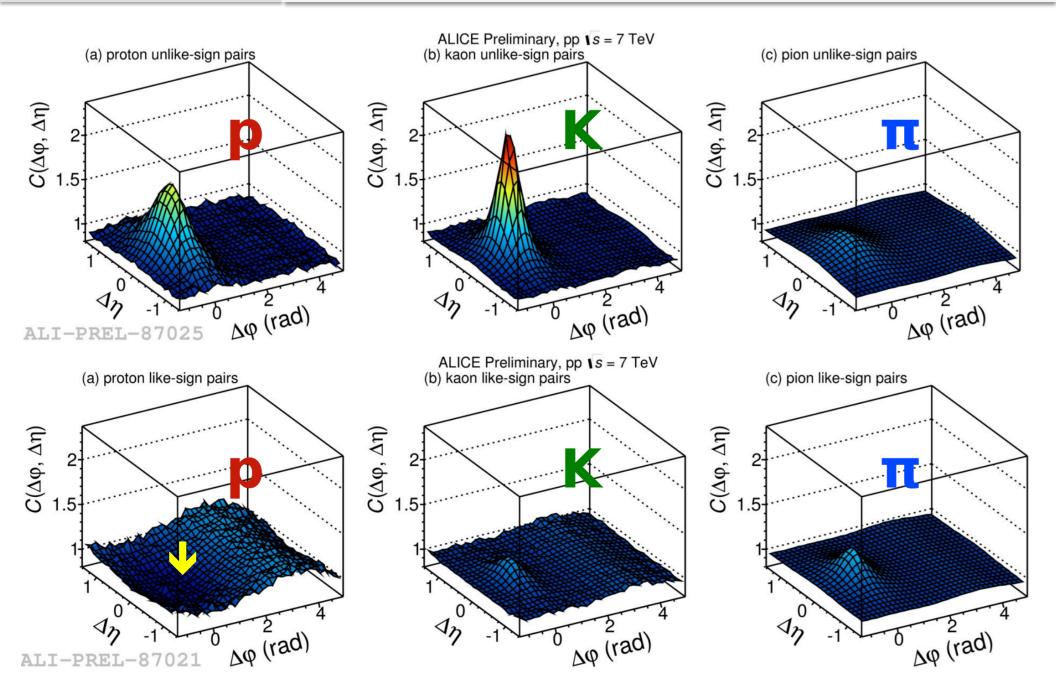
So, use 12 bins and don't show $< a_{mn} >$ for (2,4) or (4,4)

With these 3D distributions, I can then make the CF plots vs. $(\Delta y, \Delta \phi)$



Małgorzata Janik, X Workshop on Particle Correlations and Femtoscopy, Gyöngyös, Hungary, Aug 26, 2014





Małgorzata Janik, X Workshop on Particle Correlations and Femtoscopy, Gyöngyös, Hungary, Aug 26, 2014



Minijet peak at $(\Delta y, \Delta \varphi) \sim (0,0)$ seen for all PID'd pairs *except* LS protons...

 $\Delta \varphi$ dependence is $-\cos(\Delta \varphi)$ so consistent with momentum conservation...

But comparison with models with strict mom'n conservation do not have this hole (?!?)



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In RHIC BES data. another possibility is lack of available energy to create nearby 2nd baryon...

This idea used to describe e⁺e⁻ data at 20-30 GeV



From mechanism of jet production: Two primary hadrons with the same baryon number (or charge or strangeness) are separated by at least

two steps in rank ("rapidity").

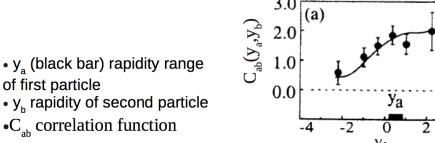
A Parametrization of the Properties of Quark Jets R.D. Field, R.P. Feynman (Caltech). Nov 1977. 131 pp. Published in Nucl. Phys. B136 (1978) 1

To conservations of the quantum numbers:

- global conservation
- local conservation

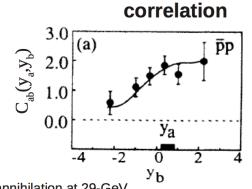
We are not likely to find two baryons or two antibaryons at the same rapidity.

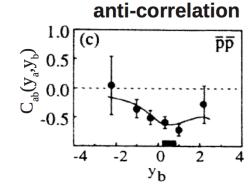
Małgorzata Janik, X Workshop on Particle Correlations and Femtoscopy, Gyöngyös, Hungary, Aug 26, 2014



 y_b Study of baryon correlations in e+e- annihilation at 29-GeV TPC/Two Gamma Collaboration (H. Aihara et al.), Phys.Rev.Lett. 57 (1986) 3140 26/08/2014, WPCF '14

Małgorzata Janik – Warsaw University of Technology





Turning now to the ☆ data...

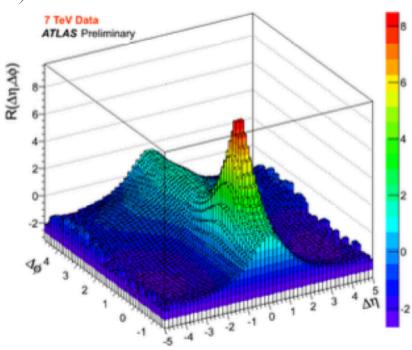
Caveats...

Hard cut to remove effects from track merging (reflection might be better)

Denominator from mixing (convolution might be better)

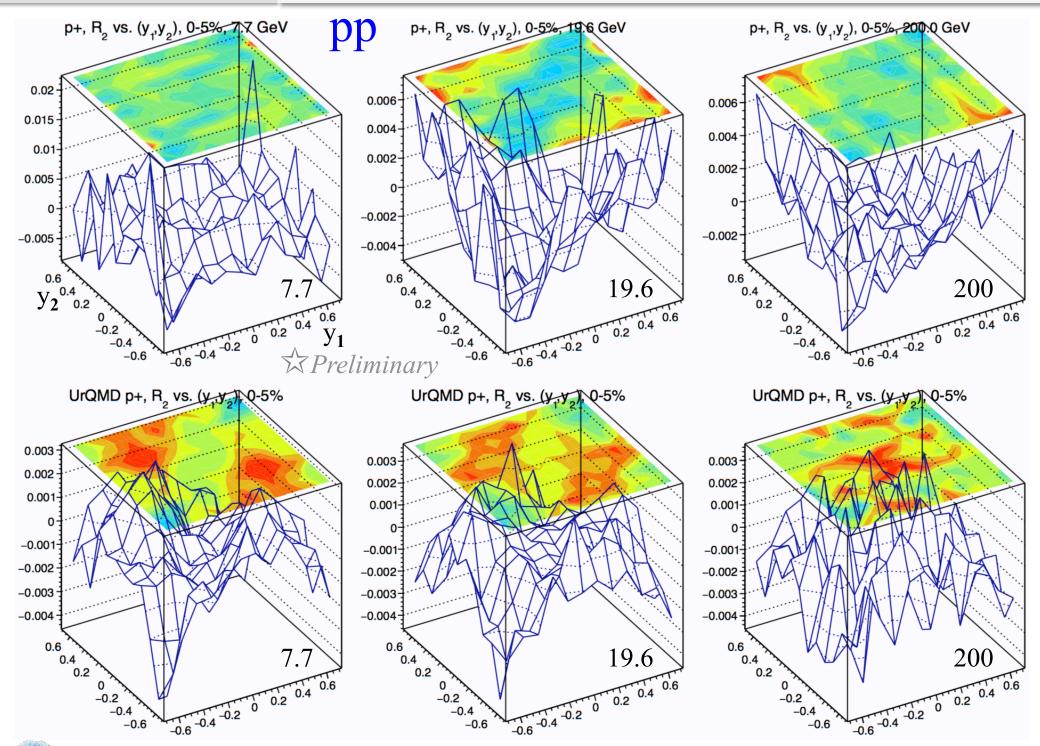
Not yet scaling R₂ by N_{part}

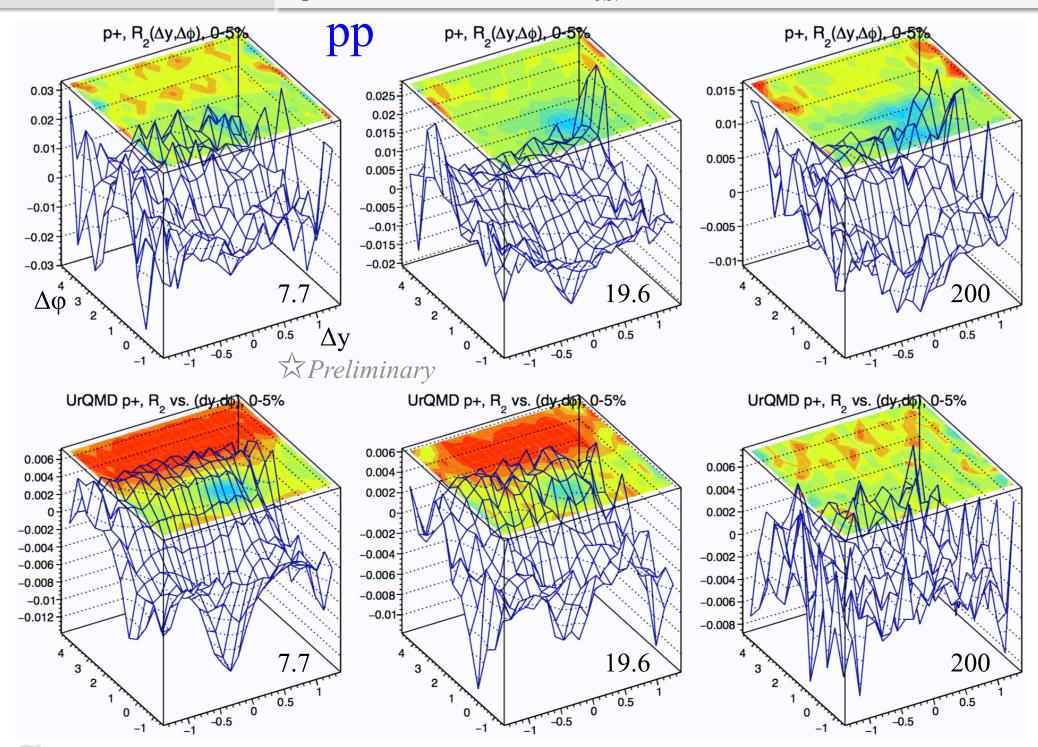
Systematic uncertainities not yet determined.

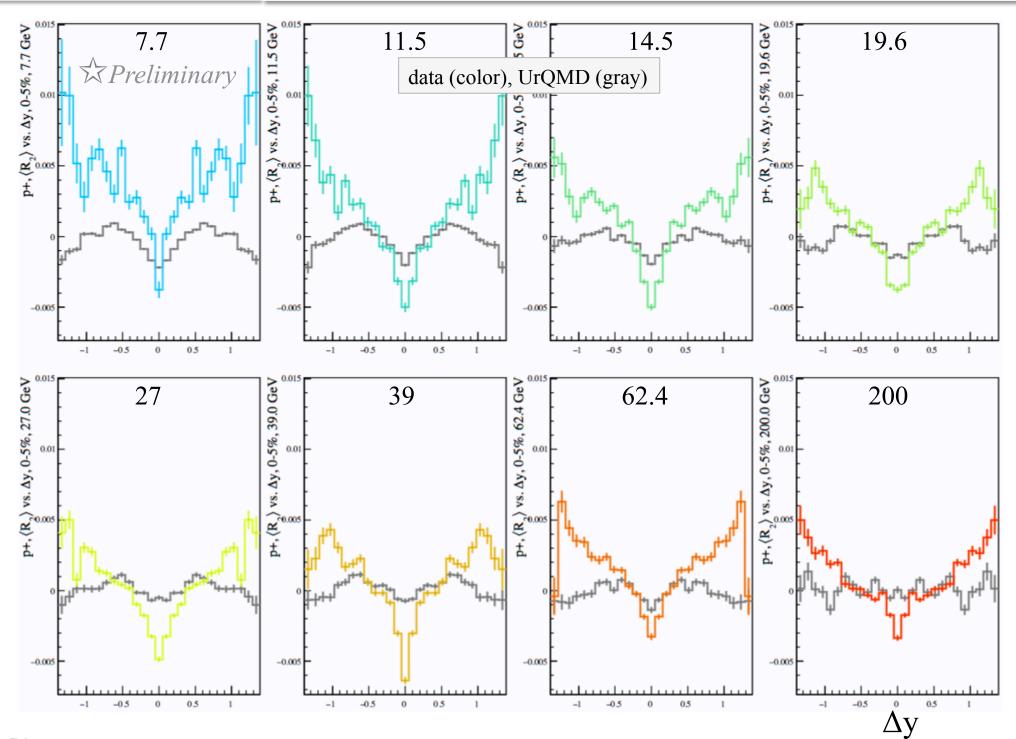


Don't expect beautifully smooth plots like produced at the LHC. Event sample sizes are similar, but the LHC has *many* more pairs/event.

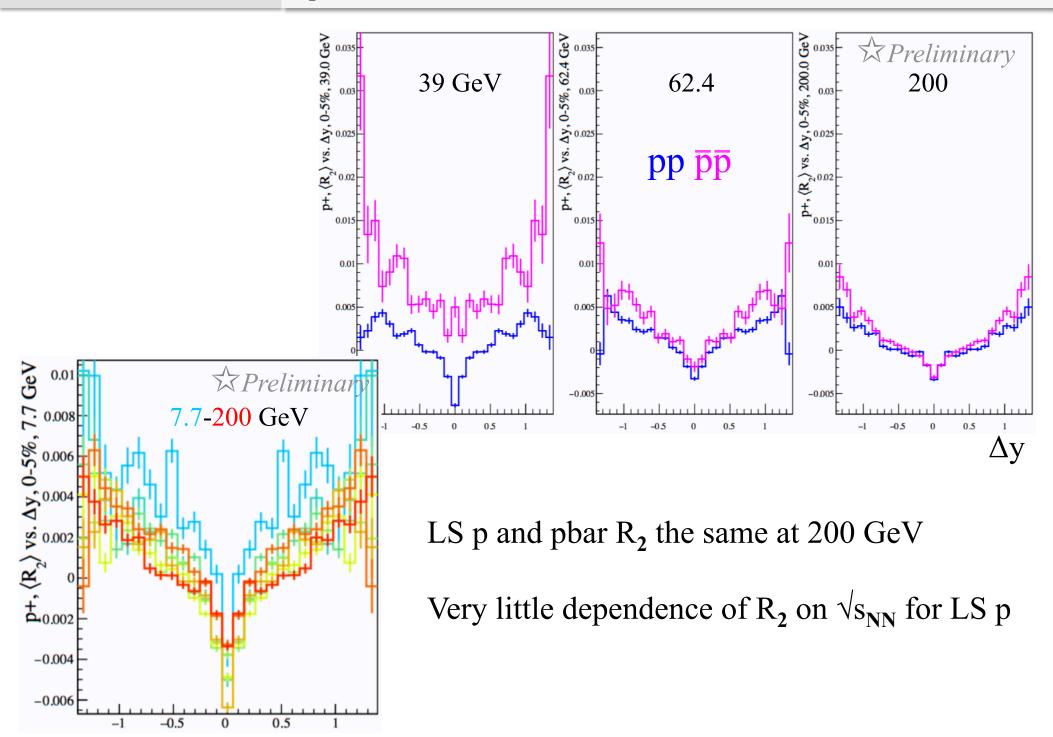




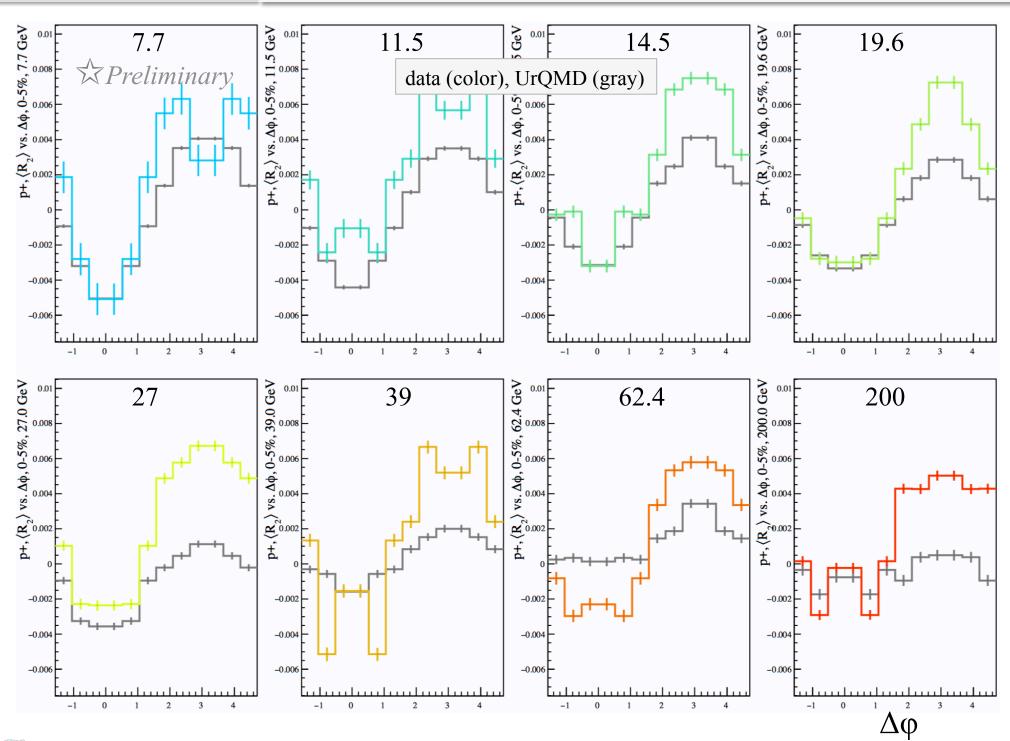




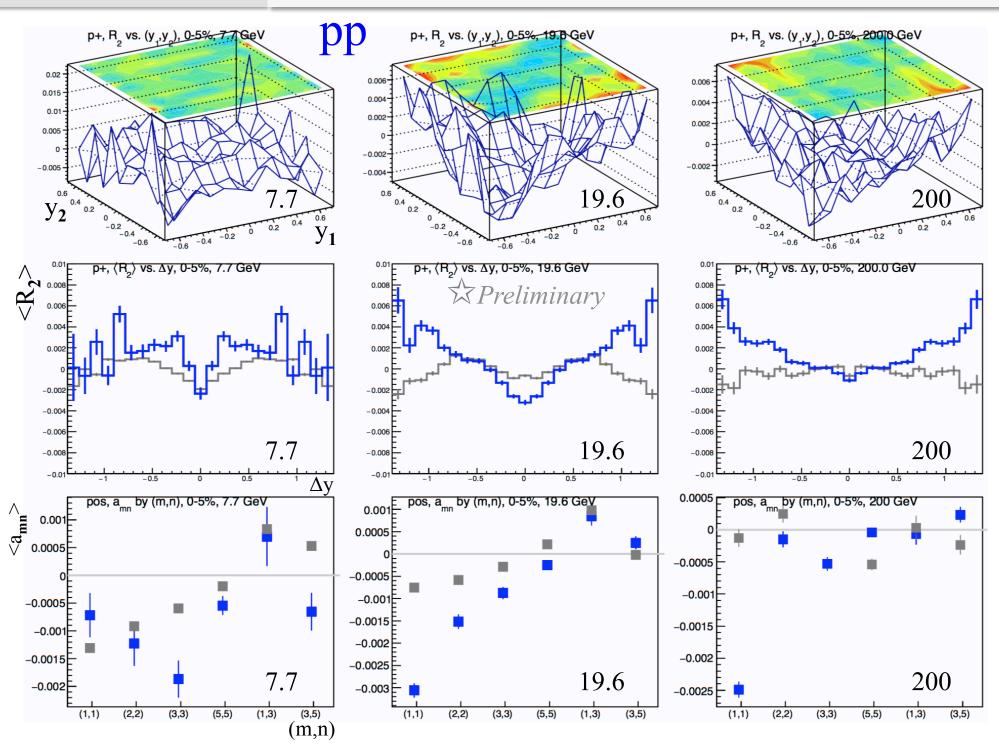




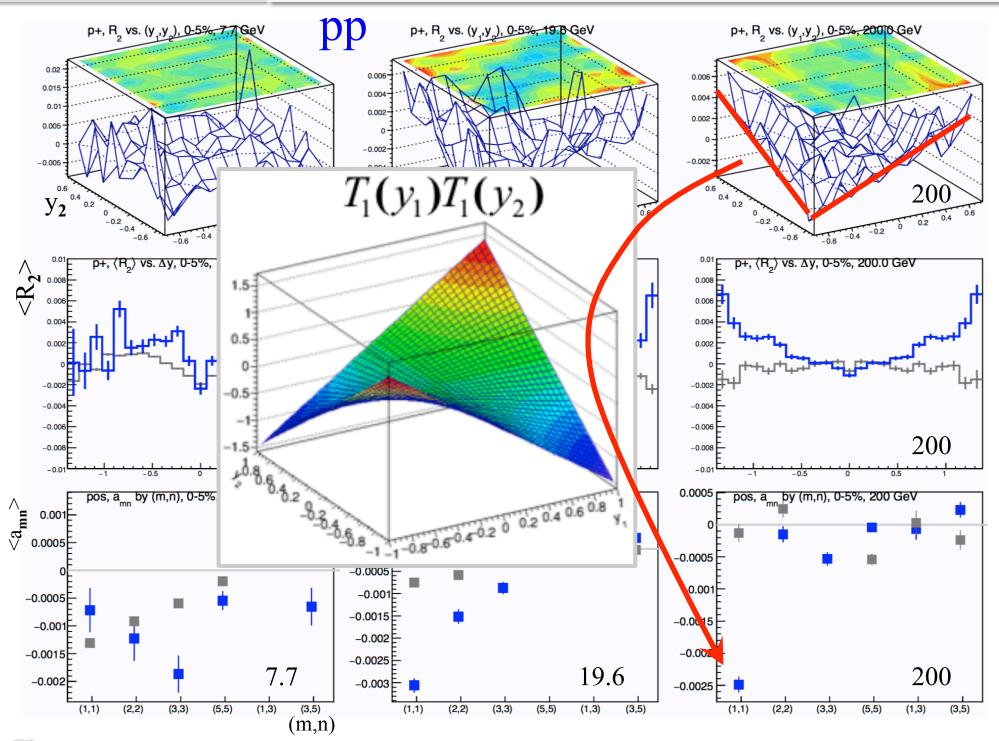




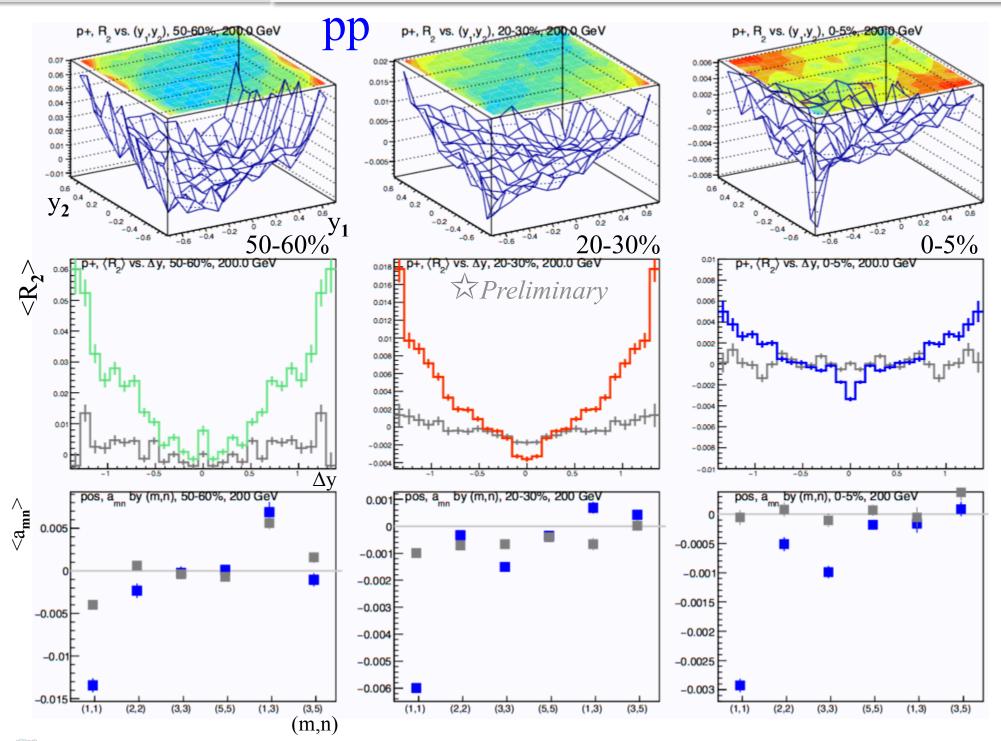


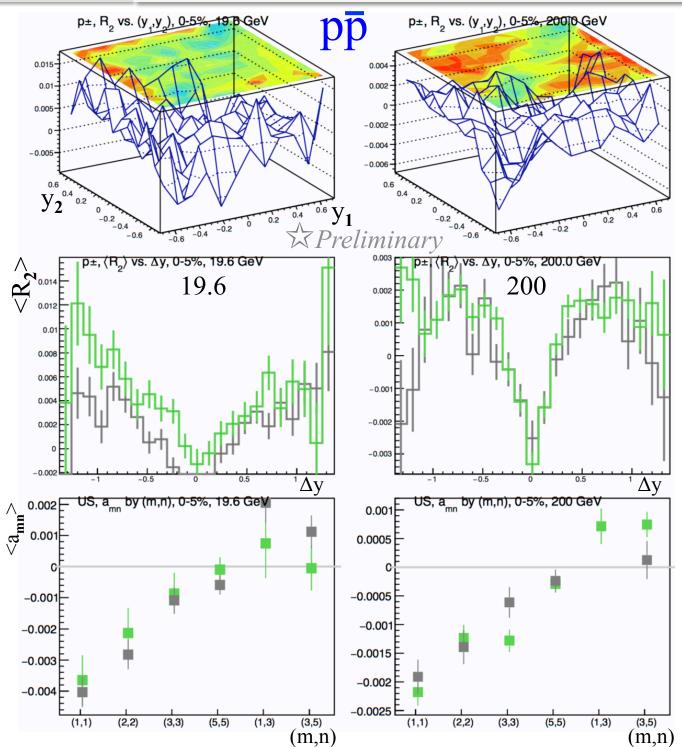




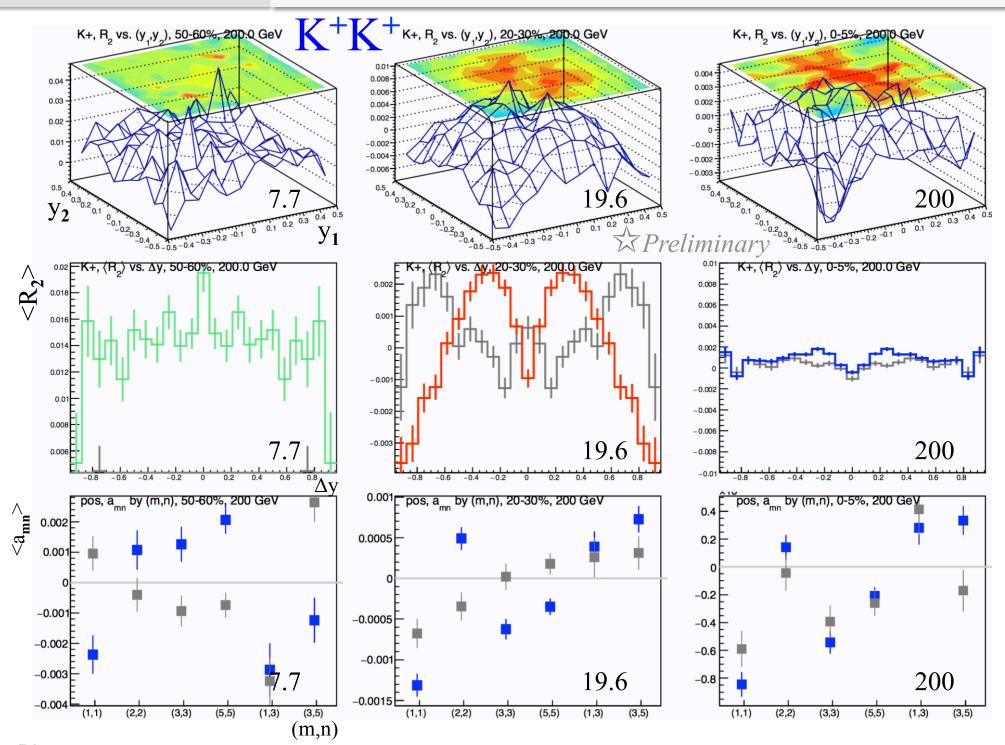














Rapidity correlation variables R_2 and C_N studied for LS and US h, K, and p as a function of the centrality and $\sqrt{s_{NN}}$

 C_N can be decomposed using basis set of Legendre polynomials to quantify the importance of different shaped (anti)correlations.

This approach is the analog in the rapidity direction of quantifying azimuthal anistropies with v_n observables.

Both STAR BES data and large samples of UrQMD events analyzed.

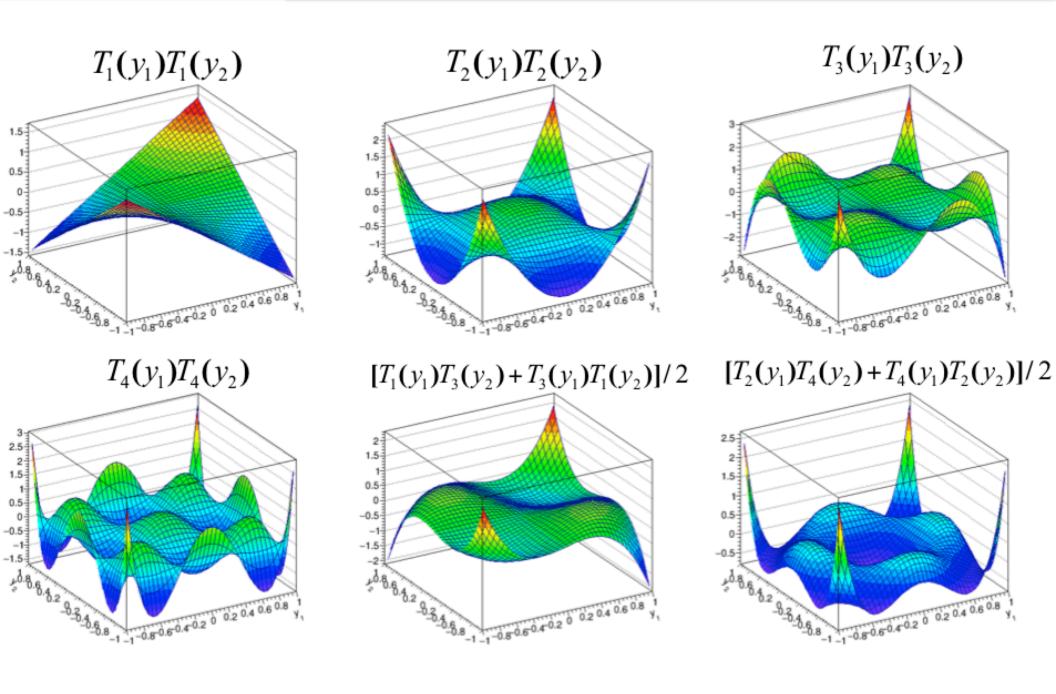
Careful run and event QA, experiment efficiencies applied to UrQMD events

Signal everywhere.

UrQMD generally does not reproduce the observations.

Would very much appreciate any thoughts!





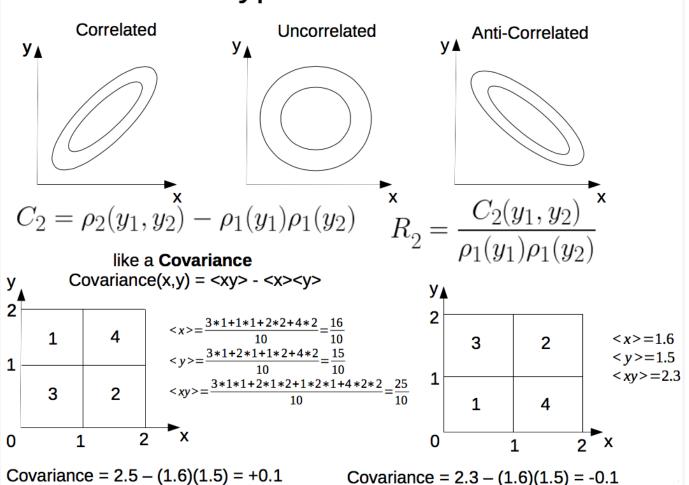


Let's look at the correlations in a different way.

$$C_2 = \rho_2(y_1, y_2) - \rho_1(y_1)\rho_1(y_2)$$

$$R_2 = \frac{C_2(y_1, y_2)}{\rho_1(y_1)\rho_1(y_2)} = \frac{\rho_2(y_1, y_2)}{\rho_1(y_1)\rho_1(y_2)} - 1$$

Three Types of Correlations



C₂ is a covariance R₂ is the covariance per pair

Correlated: $C_2,R_2>0$ Uncorrelated: $C_2,R_2\sim0$ AntiCorrelated $C_2,R_2<0$

Magnitude normalization:

$$R_2^{bs} = \frac{\left\langle n(n-1)\right\rangle}{\langle n\rangle^2} - 1$$

PHYSICAL REVIEW A

VOLUME 43, NUMBER 6

 R_k

15 MARCH 1991

Structure of correlation functions

P. Carruthers

Department of Physics, University of Arizona, Tucson, Arizona 85721 (Received 9 October 1990)

$$\begin{split} C_2(x_1, x_2) &= \rho_2(x_1, x_2) - \rho_1(x_1) \rho_1(x_2) \;, \\ C_3(x_1, x_2, x_3) &= \rho_3(x_1, x_2, x_3) - \sum_{(3)} \rho_2(x_1, x_2) \rho_1(x_3) + 2\rho_1(x_1) \rho_1(x_2) \rho_1(x_3) \;, \\ C_4(x_1, x_2, x_3, x_4) &= \rho_4(x_1, x_2, x_3, x_4) - \sum_{(4)} \rho_3(x_1, x_2, x_3) \rho_1(x_4) - \sum_{(3)} \rho_2(x_1, x_2) \rho_2(x_3, x_4) \\ &+ 2 \sum_{(6)} \rho_2(x_1, x_2) \rho_1(x_3) \rho_1(x_4) - 6\rho_1(x_1) \rho_1(x_2) \rho_1(x_3) \rho_1(x_4) \;. \end{split}$$

See also:

L. Foà, Phys. Lett. C22, 1 (1975)

H. Bøggild, Ann. Rev. Nucl. Sci. 24, 451 (1974)

M. Jacob, Phys. Rep. **315**, 7 (1999)

Lower-order correlations explicitly removed.

 R_k is just these rapidity cumulants C_k scaled by the number of pairs, triplets, quadruplets, ... R_k thus manifestly independent of experimental inefficiencies by definition...

R₂ baseline:
$$R_3 = \frac{\langle n(n-1) \rangle}{\langle n \rangle^2} - 1$$
 R₃ baseline: $R_3 = \frac{\langle n(n-1)(n-2) \rangle}{\langle n \rangle^3} - 3\frac{\langle n(n-1) \rangle}{\langle n \rangle^3} \langle n \rangle + 2$

Robust indicator of N-fold (anti)correlations, explicitly as a function of Δy and $\langle y \rangle$...

By construction, independent of single-particle inefficiencies...

