NEUTRINOS IN NUCLEAR PHYSICS

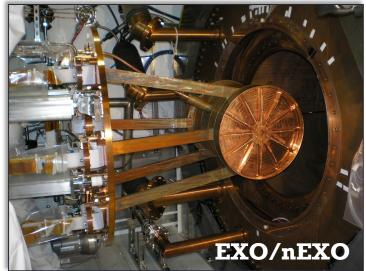
BJPJ



THE ZOO OF ONUBB SEARCHES



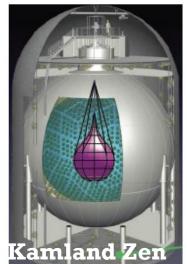


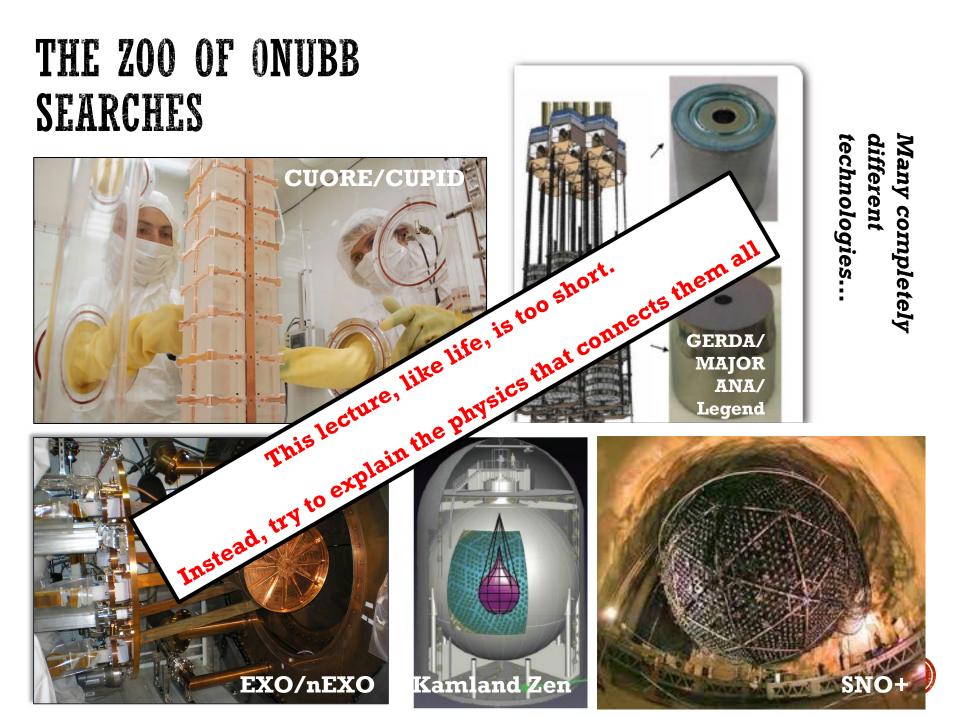


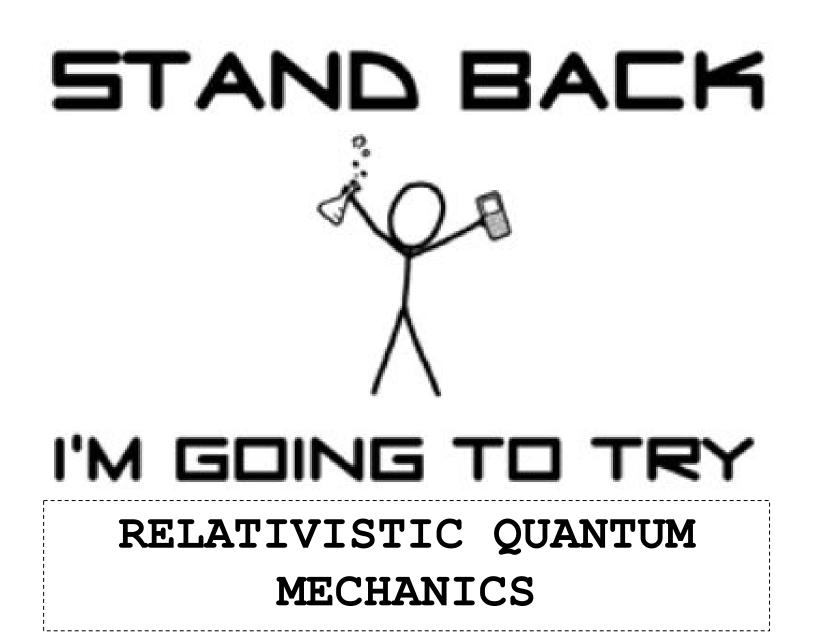


Many completely

different







DIRAC EQUATION

Spin $\frac{1}{2}$ fermions satisfy an equation of motion called the Dirac equation:

$$i\gamma^{\mu}\partial_{\mu} - m)\Psi = 0$$

The Schrodinger Eq. of
relativistic spin ½ fermions

The solution can be written as an object with four components called a Dirac spinor: (ψ_1)

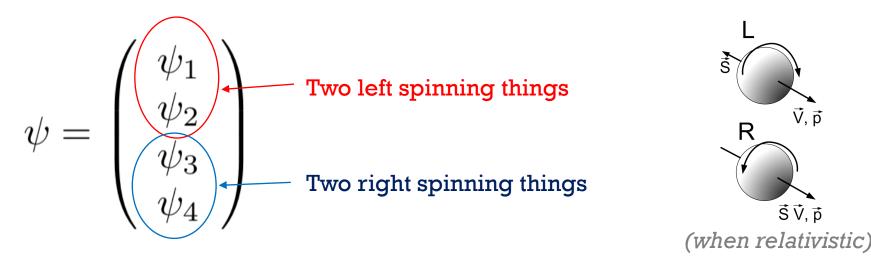
$$\Psi = \psi e^{ikx} \qquad \psi = \begin{pmatrix} \psi_1 \\ \psi_2 \\ \psi_3 \\ \psi_4 \end{pmatrix}$$

???

How much of this kind of particle is where

WHAT DO THE FOUR DEGREES OF FREEDOM OF THE DIRAC SPINOR MEAN?

• With a judicious choice of basis (Weyl):

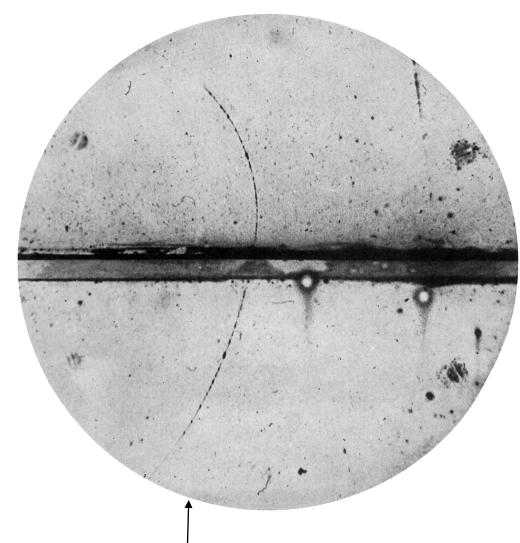


 Dirac spinor breaks into two components for a spin-up particle and two components for a spin-down particle.

But why are there two kinds of field for each spin?



ANTIMATTER



First positron detection, 1932

- Each pair has a positive energy part and a negative energy part.
- The negative energy part represents antimatter.
 - Matter moving backward in time, according to the Feynman Stueckelberg interpretation.

$$\Psi = \Psi_0 \mathbf{e}^{-\mathbf{i} \mathbf{E} \mathbf{t} / \hbar}$$

 The positron is the electrons antiparticle. It was predicted by Dirac (1928) before it was discovered by Anderson (1932).



NOT SO FAST!

Four numbers at each point in space? I'll do it with two!

But, Ettore Majorana found a new class of solutions to Dirac's equation using only two degrees of freedom.

$$\psi = \left[\begin{array}{c} \omega \\ -i\sigma_2 \omega^* \end{array} \right]$$

Four-component object built using some two-component

$$\omega = \left(egin{array}{c} \omega_1 \ \omega_2 \end{array}
ight)$$



Ettore Majorana

CHARGE CONJUGATION

$$\psi_c \equiv -i\gamma^2 \psi^*$$
 –

Definition of charge conjugation operation: transform particles $\leftarrow \rightarrow$ antiparticles

• For Majorana's solution:

$$\psi_c = \psi$$

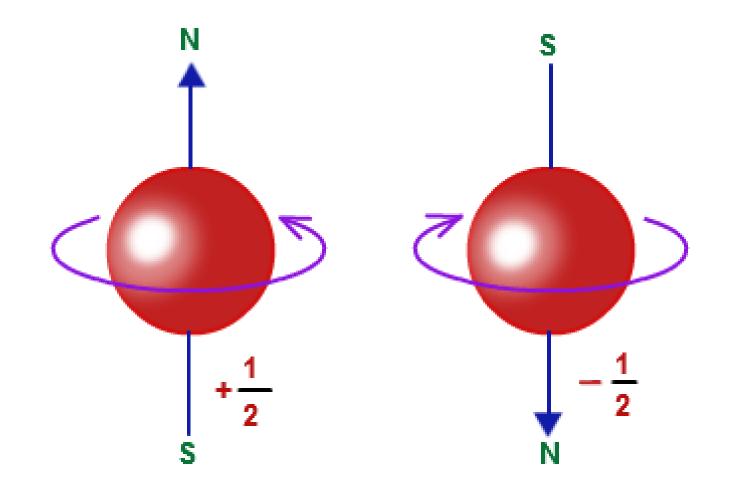
- It's antiparticle is the particle!
 Two degrees of freedom correspond to left and right of a "particle-antiparticle-thing"
- Whereas for a general Dirac solution:

$$\psi_c \neq \psi$$

Distinct particle and antiparticle
 Four degrees of freedom correspond to
 left and right of particle and antiparticle.



IN SHORT, WHAT ARE MAJORANA FERMIONS:



We call it a particle (behaves like matter)

We call it an antiparticle (behaves like antimatter)



WHO CARES?



 $-\tfrac{1}{2}\partial_{\nu}g^a_{\mu}\partial_{\nu}g^a_{\mu} - g_s f^{abc}\partial_{\mu}g^a_{\nu}g^b_{\mu}g^c_{\nu} - \tfrac{1}{4}g^2_s f^{abc}f^{ade}g^b_{\mu}g^c_{\nu}g^d_{\mu}g^e_{\nu} +$ $\frac{1}{2}ig_s^2(\bar{q}_i^\sigma\gamma^\mu q_j^\sigma)g_\mu^a + \bar{G}^a\partial^2 G^a + g_s f^{abc}\partial_\mu \bar{G}^a G^b g_\mu^c - \partial_\nu W_\mu^+ \partial_\nu W_\mu^- M^{2}W_{\mu}^{+}W_{\mu}^{-} - \frac{1}{2}\partial_{\nu}Z_{\mu}^{0}\partial_{\nu}Z_{\mu}^{0} - \frac{1}{2c_{*}^{2}}M^{2}Z_{\mu}^{0}Z_{\mu}^{0} - \frac{1}{2}\partial_{\mu}A_{\nu}\partial_{\mu}A_{\nu} - \frac{1}{2}\partial_{\mu}H\partial_{\mu}H - \frac{1}{2}\partial_{\mu}H\partial_{$ $\frac{1}{2}m_{h}^{2}H^{2}-\partial_{\mu}\phi^{+}\partial_{\mu}\phi^{-}-M^{2}\phi^{+}\bar{\phi^{-}}-\frac{1}{2}\partial_{\mu}\phi^{0}\partial_{\mu}\phi^{0}-\frac{1}{2c_{\omega}^{2}}M\phi^{0}\phi^{0}-\beta_{h}[\frac{2M^{2}}{a^{2}}+$ $\frac{2M}{g}H + \frac{1}{2}(H^2 + \phi^0\phi^0 + 2\phi^+\phi^-)] + \frac{2M^4}{g^2}\alpha_h - igc_w[\partial_\nu Z^0_\mu(W^+_\mu W^-_\nu \begin{array}{l} W_{\nu}^{+}W_{\mu}^{-}) - Z_{\nu}^{0}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{-}\partial_{\nu}W_{\mu}^{+}) + Z_{\mu}^{0}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\nu}^{-}\partial_{\nu}W_{\mu}^{+})] - igs_{w}[\partial_{\nu}A_{\mu}(W_{\mu}^{+}W_{\nu}^{-} - W_{\nu}^{+}W_{\mu}^{-}) - A_{\nu}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\nu}^{-}W_{\nu}^{-})] \\ \end{array}$ $\begin{array}{l} W^-_\mu \partial_\nu W^+_\mu) + A_\mu (W^+_\nu \partial_\nu W^-_\mu - W^-_\nu \partial_\nu W^+_\mu)] - \frac{1}{2}g^2 W^+_\mu W^-_\mu W^+_\nu W^-_\nu + \\ \frac{1}{2}g^2 W^+_\mu W^-_\nu W^+_\mu W^-_\nu + g^2 c^2_w (Z^0_\mu W^+_\mu Z^0_\nu W^-_\nu - Z^0_\mu Z^0_\mu W^+_\nu W^-_\nu) + \\ g^2 s^2_w (A_\mu W^+_\mu A_\nu W^-_\nu - A_\mu A_\mu W^+_\nu W^-_\nu) + g^2 s_w c_w [A_\mu Z^0_\nu (W^+_\mu W^-_\nu - W^-_\mu Q^0_\nu W^+_\nu W^-_\nu] + \\ \end{array}$ $W^+_{\nu}W^-_{\mu}) - 2A_{\mu}Z^0_{\mu}W^+_{\nu}W^-_{\nu}] - g\alpha[H^3 + H\phi^0\phi^0 + 2H\phi^+\phi^-] \tfrac{1}{8}g^2\alpha_{\hbar}[H^4+(\phi^0)^4+4(\phi^+\phi^-)^2+4(\phi^0)^2\phi^+\phi^-+4H^2\phi^+\phi^-+2(\phi^0)^2H^2]$ $gMW^+_{\mu}W^-_{\mu}H - \frac{1}{2}g\frac{M}{c^2}Z^0_{\mu}Z^0_{\mu}H - \frac{1}{2}ig[W^+_{\mu}(\phi^0\partial_{\mu}\phi^- - \phi^-\partial_{\mu}\phi^0) - \psi^0\partial_{\mu}\phi^- - \phi^-\partial_{\mu}\phi^0]$ $W^{-}_{\mu}(\phi^{0}\partial_{\mu}\phi^{+}-\phi^{+}\partial_{\mu}\phi^{0})] + \frac{1}{2}g[W^{+}_{\mu}(H\partial_{\mu}\phi^{-}-\phi^{-}\partial_{\mu}H)-W^{-}_{\mu}(H\partial_{\mu}\phi^{+}-\phi^{-}\partial_{\mu}H)] + \frac{1}{2}g[W^{+}_{\mu}(H\partial_{\mu}\phi^{-}-\phi^{-}\partial_{\mu}H)] + \frac{1$ $\phi^+ \partial_\mu H)] + \tfrac{1}{2} g \tfrac{1}{c_w} (Z^0_\mu (H \partial_\mu \phi^0 - \phi^0 \partial_\mu H) - i g \tfrac{s^2_w}{c_w} M Z^0_\mu (W^+_\mu \phi^- - W^-_\mu \phi^+) +$
$$\begin{split} & igs_w MA_\mu (W^+_\mu \phi^- - W^-_\mu \phi^+) - ig \frac{1 - 2c_w^2}{2c_w} Z^0_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + \\ & igs_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) - \frac{1}{4} g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \end{split}$$
 $\frac{1}{4}g^2 \frac{1}{c^2} Z^0_\mu Z^0_\mu [H^2 + (\phi^0)^2 + 2(2s^2_w - 1)^2 \phi^+ \phi^-] - \frac{1}{2}g^2 \frac{s^2_w}{c_w} Z^0_\mu \phi^0 (W^+_\mu \phi^- +$ $W^{-}_{\mu}\phi^{+}) - \frac{1}{2}ig^{2}\frac{s_{\mu}^{2}}{c_{\mu}}Z^{0}_{\mu}H(W^{+}_{\mu}\phi^{-} - W^{-}_{\mu}\phi^{+}) + \frac{1}{2}g^{2}s_{w}A_{\mu}\phi^{0}(W^{+}_{\mu}\phi^{-} +$ $W^{-}_{\mu}\phi^{+}) + \frac{1}{2}ig^{2}s_{w}A_{\mu}H(W^{+}_{\mu}\phi^{-} - W^{-}_{\mu}\phi^{+}) - g^{2}\frac{s_{w}}{c_{w}}(2c_{w}^{2} - 1)Z^{0}_{\mu}A_{\mu}\phi^{+}\phi^{-} - W^{-}_{\mu}\phi^{+})$ $q^1 s_w^2 A_\mu A_\mu \phi^+ \phi^- - \bar{e}^{\lambda} (\gamma \partial + m_{\lambda}^{\lambda}) e^{\lambda} - \bar{\nu}^{\lambda} \gamma \partial \bar{\nu}^{\lambda} - \bar{u}_{\lambda}^{\lambda} (\gamma \partial + m_{\mu}^{\lambda}) u_{\lambda}^{\lambda} \bar{d}_i^{\lambda}(\gamma\partial + m_d^{\lambda})d_i^{\lambda} + igs_w A_{\mu}[-(\bar{e}^{\lambda}\gamma^{\mu}e^{\lambda}) + \frac{2}{3}(\bar{u}_j^{\lambda}\gamma^{\mu}u_j^{\lambda}) - \frac{1}{3}(\bar{d}_j^{\lambda}\gamma^{\mu}d_j^{\lambda})] +$ $\frac{ig}{4c_w}Z^0_{\mu}[(\bar{\nu}^{\lambda}\gamma^{\mu}(1+\gamma^5)\nu^{\lambda}) + (\bar{e}^{\lambda}\gamma^{\mu}(4s_w^2 - 1 - \gamma^5)e^{\lambda}) + (\bar{u}^{\lambda}_i\gamma^{\mu}(\frac{4}{3}s_w^2 - 1 - \gamma^5)e^{\lambda}) + (\bar{u}^{\lambda}_i\gamma^{\mu}(\frac{4}{3}s_w^2 - 1 - \gamma^5)e^{\lambda}) + (\bar{u}^{\lambda}_i\gamma^{\mu}(1+\gamma^5)\nu^{\lambda}) + (\bar{e}^{\lambda}\gamma^{\mu}(1+\gamma^5)\nu^{\lambda}) + (\bar{e}^{\lambda}\gamma^{\mu}(1+\gamma^5)\nu^{$ $1 - \gamma^{5} u_{j}^{\lambda} + (\bar{d}_{j}^{\lambda} \gamma^{\mu} (1 - \frac{8}{3} s_{w}^{2} - \gamma^{5}) d_{j}^{\lambda})] + \frac{ig}{2\sqrt{2}} W_{\mu}^{+} [(\bar{\nu}^{\lambda} \gamma^{\mu} (1 + \gamma^{5}) \lambda^{\lambda}) +$ $(\bar{u}_{i}^{\lambda}\gamma^{\mu}(1+\gamma^{5})C_{\lambda\kappa}d_{j}^{\kappa})] + \frac{ig}{2\sqrt{2}}W_{\mu}^{-}[(\bar{e}^{\lambda}\gamma^{\mu}(1+\gamma^{5})\nu^{\lambda}) + (\bar{d}_{j}^{\kappa}C_{\lambda\kappa}^{\dagger}\gamma^{\mu}(1+\gamma^{5})\nu^{\lambda})]$ $\gamma^{5}(u_{j}^{\lambda})] + \frac{ig}{2\sqrt{2}} \frac{m_{e}^{\lambda}}{M} [-\phi^{+}(\bar{\nu}^{\lambda}(1-\gamma^{5})e^{\lambda}) + \phi^{-}(\bar{e}^{\lambda}(1+\gamma^{5})\nu^{\lambda})] \frac{g}{2}\frac{m_{\epsilon}^{\lambda}}{M}[H(\bar{e}^{\lambda}e^{\lambda}) + i\phi^{0}(\bar{e}^{\lambda}\gamma^{5}e^{\lambda})] + \frac{ig}{2M\sqrt{2}}\phi^{+}[-m_{d}^{\kappa}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1-\gamma^{5})d_{j}^{\kappa}) +$ $m_u^{\lambda}(\bar{u}_i^{\lambda}C_{\lambda\kappa}(1+\gamma^5)d_i^{\kappa}] + \frac{ig}{2M_s/2}\phi^{-}[m_d^{\lambda}(\bar{d}_i^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_i^{\kappa}) - m_u^{\kappa}(\bar{d}_i^{\lambda}C_{\lambda\kappa}^{\dagger}(1-\gamma^5)u_i^{\kappa})]$ $\gamma^5 u_j^\kappa = -\frac{g}{2} \frac{m_u^\lambda}{M} H(\bar{u}_j^\lambda u_j^\lambda) - \frac{g}{2} \frac{m_d^\lambda}{M} H(\bar{d}_j^\lambda d_j^\lambda) + \frac{ig}{2} \frac{m_u^\lambda}{M} \phi^0(\bar{u}_j^\lambda \gamma^5 u_j^\lambda) - \frac{g}{2} \frac{m_u^\lambda}{M} \phi^0(\bar{u}_j^\lambda \gamma^5 u_j^\lambda) - \frac{g}{2} \frac{m_d^\lambda}{M} H(\bar{d}_j^\lambda d_j^\lambda) + \frac{ig}{2} \frac{m_u^\lambda}{M} \phi^0(\bar{u}_j^\lambda \gamma^5 u_j^\lambda) - \frac{g}{2} \frac{m_u^\lambda}{M} H(\bar{d}_j^\lambda d_j^\lambda) + \frac{ig}{2} \frac{m_u^\lambda}{M} \phi^0(\bar{u}_j^\lambda \gamma^5 u_j^\lambda) - \frac{g}{2} \frac{m_u^\lambda}{M} H(\bar{d}_j^\lambda d_j^\lambda) + \frac{ig}{2} \frac{m_u^\lambda}{M} \phi^0(\bar{u}_j^\lambda \gamma^5 u_j^\lambda) - \frac{g}{2} \frac{m_u^\lambda}{M} H(\bar{d}_j^\lambda d_j^\lambda) + \frac{ig}{2} \frac{m_u^\lambda}{M} \phi^0(\bar{u}_j^\lambda \gamma^5 u_j^\lambda) - \frac{g}{2} \frac{m_u^\lambda}{M} H(\bar{d}_j^\lambda d_j^\lambda) + \frac{ig}{2} \frac{m_u^\lambda}{M} \phi^0(\bar{u}_j^\lambda \gamma^5 u_j^\lambda) - \frac{g}{2} \frac{m_u^\lambda}{M} H(\bar{d}_j^\lambda d_j^\lambda) + \frac{ig}{2} \frac{m_u^\lambda}{M} \phi^0(\bar{u}_j^\lambda \gamma^5 u_j^\lambda) - \frac{g}{2} \frac{m_u^\lambda}{M} H(\bar{d}_j^\lambda d_j^\lambda) + \frac{ig}{2} \frac{m_u^\lambda}{M} \phi^0(\bar{u}_j^\lambda \gamma^5 u_j^\lambda) - \frac{g}{2} \frac{m_u^\lambda}{M} \phi^0(\bar{u}_j^\lambda \gamma^5 u_j^\lambda) + \frac{ig}{2} \frac{m_u^\lambda}{M} \phi^0(\bar{u}_j^\lambda \gamma^5 u_j^\lambda) - \frac{g}{2} \frac{m_u^\lambda}{M} \phi^0(\bar{u}_j^\lambda \gamma^5 u_j^\lambda) + \frac{ig}{2} \frac{m_u^\lambda}{M} \phi^0(\bar{u}$ $\frac{ig}{2}\frac{m_{\tilde{d}}^{\lambda}}{M}\phi^0(\bar{d}_j^{\lambda}\gamma^5d_j^{\lambda}) + \bar{X}^+(\partial^2 - M^2)X^+ + \bar{X}^-(\partial^2 - M^2)X^- + \bar{X}^0(\partial^2 \frac{M^2}{c^2}$) X^0 + $\overline{Y}\partial^2 Y$ + $igc_w W^+_\mu (\partial_\mu \overline{X}^0 X^- - \partial_\mu \overline{X}^+ X^0)$ + $igs_w W^+_\mu (\partial_\mu \overline{Y} X^- - \partial_\mu \overline{X}^+ X^0)$ + $igs_w W^+_\mu (\partial_\mu \overline{Y} X^- - \partial_\mu \overline{X}^+ X^0)$ $\partial_{\mu}\bar{X}^{+}Y) + igc_{w}W^{-}_{\mu}(\partial_{\mu}\bar{X}^{-}X^{0} - \partial_{\mu}\bar{X}^{0}X^{+}) + igs_{w}W^{-}_{\mu}(\partial_{\mu}\bar{X}^{-}Y - \partial_{\mu}\bar{X}^{0}X^{+}))$ $\partial_{\mu}\bar{Y}X^{+}) + igc_{w}Z^{0}_{\mu}(\partial_{\mu}\bar{X}^{+}X^{+} - \partial_{\mu}\bar{X}^{-}X^{-}) + igs_{w}A_{\mu}(\partial_{\mu}\bar{X}^{+}X^{+} - \partial_{\mu}\bar{X}^{-}X^{-}) + igs_{w}A_{\mu}(\partial_{\mu}\bar{X}^{+}X^{+}) + igs_{w$ $\partial_{\mu}\bar{X}^{-}X^{-}) - \frac{1}{2}gM[\bar{X}^{+}X^{+}H + \bar{X}^{-}X^{-}H + \frac{1}{c^{2}}\bar{X}^{0}X^{0}H] +$ $\frac{1-2c_w^2}{2c_w}igM[\bar{X}^+X^0\phi^+ - \bar{X}^-X^0\phi^-] + \frac{1}{2c_w}igM[\bar{X}^0X^-\phi^+ - \bar{X}^0X^+\phi^-] +$ $igMs_w[\bar{X}^0X^-\phi^+ - \bar{X}^0X^+\phi^-] + \frac{1}{2}igM[\bar{X}^+X^+\phi^0 - \bar{X}^-X^-\phi^0]$

The standard model Lagrangian

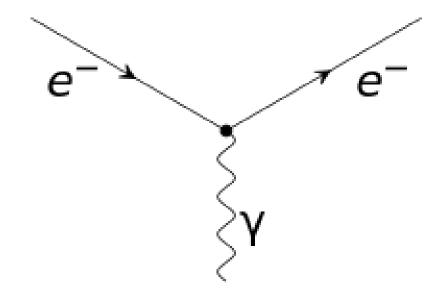
Each term represents some interaction between quantum fields.

After quantizing the theory, this becomes an interaction between particles.



 $-\frac{1}{2}\partial_{\nu}g^a_{\mu}\partial_{\nu}g^a_{\mu} - g_s f^{abc}\partial_{\mu}g^a_{\nu}g^b_{\mu}g^c_{\nu} - \frac{1}{4}g^2_s f^{abc}f^{ade}g^b_{\mu}g^c_{\nu}g^d_{\mu}g^e_{\nu} +$ $\frac{1}{2}ig_s^2(\bar{q}_i^\sigma\gamma^\mu q_j^\sigma)g_\mu^a + \bar{G}^a\partial^2 G^a + g_s f^{abc}\partial_\mu \bar{G}^a G^b g_\mu^c - \partial_\nu W_\mu^+ \partial_\nu W_\mu^- M^{2}W^{+}_{\mu}W^{-}_{\mu} - \frac{1}{2}\partial_{\nu}Z^{0}_{\mu}\partial_{\nu}Z^{0}_{\mu} - \frac{1}{2c^{2}_{w}}M^{2}Z^{0}_{\mu}Z^{0}_{\mu} - \frac{1}{2}\partial_{\mu}A_{\nu}\partial_{\mu}A_{\nu} - \frac{1}{2}\partial_{\mu}H\partial_{\mu}H - \frac{1}{2}\partial_{\mu}H\partial_{$ $\tfrac{1}{2}m_{h}^{2}H^{2} - \partial_{\mu}\phi^{+}\partial_{\mu}\phi^{-} - M^{2}\phi^{+}\phi^{-} - \tfrac{1}{2}\partial_{\mu}\phi^{0}\partial_{\mu}\phi^{0} - \tfrac{1}{2c_{w}^{2}}M\phi^{0}\phi^{0} - \beta_{h}[\tfrac{2M^{2}}{g^{2}} +$ $\frac{2M}{g}H + \frac{1}{2}(H^2 + \phi^0\phi^0 + 2\phi^+\phi^-)] + \frac{2M^4}{g^2}\alpha_h - igc_w[\partial_\nu Z^0_\mu(W^+_\mu W^-_\nu - \psi^+_\mu W^+_\nu - \psi^+_\mu W^+_\mu W^+_\nu - \psi^+_\mu W^+_\mu W$ $\begin{array}{l} W_{\nu}^{+}W_{\mu}^{-}) - Z_{\nu}^{0}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{-}\partial_{\nu}W_{\mu}^{+}) + Z_{\mu}^{0}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\nu}^{-}\partial_{\nu}W_{\mu}^{+})] - igs_{w}[\partial_{\nu}A_{\mu}(W_{\mu}^{+}W_{\nu}^{-} - W_{\nu}^{+}W_{\mu}^{-}) - A_{\nu}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\nu}^{-}W_{\nu}^{-})] \\ \end{array}$ $W^{-}_{\mu}\partial_{\nu}W^{+}_{\mu}) + A_{\mu}(W^{+}_{\nu}\partial_{\nu}W^{-}_{\mu} - W^{-}_{\nu}\partial_{\nu}W^{+}_{\mu})] - \frac{1}{2}g^{2}W^{+}_{\mu}W^{-}_{\nu}W^{+}_{\nu}W^{-}_{\nu} + C^{2}_{\mu}W^{+}_{\mu}W^{-}_{\nu}W^{+}_{\mu}W^{-}_{\mu}W^{+}_{\mu}W^{+}_{$ ${\textstyle\frac{1}{2}}g^2W^{\mu}_{\mu}W^{-}_{\nu}W^{+}_{\mu}W^{-}_{\nu}+g^2c^2_w(Z^0_{\mu}W^{+}_{\mu}Z^0_{\nu}W^{-}_{\nu}-Z^0_{\mu}Z^0_{\mu}W^{+}_{\nu}W^{-}_{\nu})+$ $g^{2}s_{w}^{2}(A_{\mu}W_{\mu}^{+}A_{\nu}W_{\nu}^{-} - A_{\mu}A_{\mu}W_{\nu}^{+}W_{\nu}^{-}) + g^{2}s_{w}c_{w}[A_{\mu}Z_{\nu}^{0}(W_{\mu}^{+}W_{\nu}^{-} - A_{\mu}A_{\mu}W_{\nu}^{+}W_{\nu}^{-})]$ $W^+_{\nu}W^-_{\mu}) - 2A_{\mu}Z^0_{\mu}W^+_{\nu}W^-_{\nu}] - g\alpha[H^3 + H\phi^0\phi^0 + 2H\phi^+\phi^-] \frac{1}{8}g^2\alpha_{\hbar}[H^4 + (\phi^0)^4 + 4(\phi^+\phi^-)^2 + 4(\phi^0)^2\phi^+\phi^- + 4H^2\phi^+\phi^- + 2(\phi^0)^2H^2]$ $gMW^+_{\mu}W^-_{\mu}H - \tfrac{1}{2}g\tfrac{M}{c_{\omega}^2}Z^0_{\mu}Z^0_{\mu}H - \tfrac{1}{2}ig[W^+_{\mu}(\phi^0\partial_{\mu}\phi^- - \phi^-\partial_{\mu}\phi^0) W^{-}_{\mu}(\phi^{0}\partial_{\mu}\phi^{+}-\phi^{+}\partial_{\mu}\phi^{0})] + \frac{1}{2}g[W^{+}_{\mu}(H\partial_{\mu}\phi^{-}-\phi^{-}\partial_{\mu}H) - W^{-}_{\mu}(H\partial_{\mu}\phi^{+}-\phi^{-}\partial_{\mu}H)] + \frac{1}{2}g[W^{+}_{\mu}(H\partial_{\mu}\phi^{-}-\phi^{-}\partial_{\mu}H)] + \frac{1}{2}g[W^{+}_{\mu}(H\partial_{\mu}\phi^{-}-\phi^{-}\partial_{\mu}H)$ $\phi^+ \partial_\mu H)] + \frac{1}{2} g \frac{1}{c_w} (Z^0_\mu (H \partial_\mu \phi^0 - \phi^0 \partial_\mu H) - i g \frac{s^2_w}{c_w} M Z^0_\mu (W^+_\mu \phi^- - W^-_\mu \phi^+) +$
$$\begin{split} & igs_w MA_\mu (W^+_\mu \phi^- - W^-_\mu \phi^+) - ig \frac{1 - 2c_w^2}{2c_w} Z^0_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + \\ & igs_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) - \frac{1}{4} g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \end{split}$$
 $\frac{1}{4}g^2 \frac{1}{c_*^2} Z^0_\mu Z^0_\mu [H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2 \phi^+ \phi^-] - \frac{1}{2}g^2 \frac{s_w^2}{c_w} Z^0_\mu \phi^0 (W^+_\mu \phi^- + \phi^-) + \frac{1}{2}g^2 \frac{s_w^2}{c_*} Z^0_\mu \phi^0 (W^+_\mu \phi^- + \phi^-) + \frac{1}{2}g^2 \frac{s_w^2}{c_*} Z^0_\mu \phi^0 (W^+_\mu \phi^- + \phi^-) + \frac{1}{2}g^2 \frac{s_w^2}{c_*} Z^0_\mu \phi^0 (W^+_\mu \phi^- + \phi^-) + \frac{1}{2}g^2 \frac{s_w^2}{c_*} Z^0_\mu \phi^0 (W^+_\mu \phi^- + \phi^-) + \frac{1}{2}g^2 \frac{s_w^2}{c_*} Z^0_\mu \phi^0 (W^+_\mu \phi^- + \phi^-) + \frac{1}{2}g^2 \frac{s_w^2}{c_*} Z^0_\mu \phi^0 (W^+_\mu \phi^- + \phi^-) + \frac{1}{2}g^2 \frac{s_w^2}{c_*} Z^0_\mu \phi^0 (W^+_\mu \phi^- + \phi^-) + \frac{1}{2}g^2 \frac{s_w^2}{c_*} Z^0_\mu \phi^0 (W^+_\mu \phi^- + \phi^-) + \frac{1}{2}g^2 \frac{s_w^2}{c_*} Z^0_\mu \phi^0 (W^+_\mu \phi^- + \phi^-) + \frac{1}{2}g^2 \frac{s_w^2}{c_*} Z^0_\mu \phi^0 (W^+_\mu \phi^- + \phi^-) + \frac{1}{2}g^2 \frac{s_w^2}{c_*} Z^0_\mu \phi^0 (W^+_\mu \phi^- + \phi^-) + \frac{1}{2}g^2 \frac{s_w^2}{c_*} Z^0_\mu \phi^0 (W^+_\mu \phi^- + \phi^-) + \frac{1}{2}g^2 \frac{s_w^2}{c_*} Z^0_\mu \phi^0 (W^+_\mu \phi^- + \phi^-) + \frac{1}{2}g^2 \frac{s_w^2}{c_*} Z^0_\mu \phi^0 (W^+_\mu \phi^- + \phi^-) + \frac{1}{2}g^2 \frac{s_w^2}{c_*} Z^0_\mu \phi^0 (W^+_\mu \phi^- + \phi^-) + \frac{1}{2}g^2 \frac{s_w^2}{c_*} Z^0_\mu \phi^0 (W^+_\mu \phi^- + \phi^-) + \frac{1}{2}g^2 \frac{s_w^2}{c_*} Z^0_\mu \phi^0 (W^+_\mu \phi^- + \phi^-) + \frac{1}{2}g^2 \frac{s_w^2}{c_*} Z^0_\mu \phi^0 (W^+_\mu \phi^- + \phi^-) + \frac{1}{2}g^2 \frac{s_w^2}{c_*} Z^0_\mu \phi^0 (W^+_\mu \phi^- + \phi^-) + \frac{1}{2}g^2 \frac{s_w^2}{c_*} Z^0_\mu \phi^0 (W^+_\mu \phi^- + \phi^-) + \frac{1}{2}g^2 \frac{s_w^2}{c_*} Z^0_\mu \phi^0 (W^+_\mu \phi^- + \phi^-) + \frac{1}{2}g^2 \frac{s_w^2}{c_*} Z^0_\mu \phi^0 (W^+_\mu \phi^- + \phi^-) + \frac{1}{2}g^2 \frac{s_w^2}{c_*} Z^0_\mu \phi^0 (W^+_\mu \phi^- + \phi^-) + \frac{1}{2}g^2 \frac{s_w^2}{c_*} Z^0_\mu \phi^0 (W^+_\mu \phi^- + \phi^-) + \frac{1}{2}g^2 \frac{s_w^2}{c_*} Z^0_\mu \phi^0 (W^+_\mu \phi^- + \phi^-) + \frac{1}{2}g^2 \frac{s_w^2}{c_*} Z^0_\mu \phi^0 (W^+_\mu \phi^ W^{-}_{\mu}\phi^{+}) - \frac{1}{2}ig^{2}\frac{s^{2}_{\mu}}{c_{w}}Z^{0}_{\mu}H(W^{+}_{\mu}\phi^{-} - W^{-}_{\mu}\phi^{+}) + \frac{1}{2}g^{2}s_{w}A_{\mu}\phi^{0}(W^{+}_{\mu}\phi^{-} + W^{-}_{\mu}\phi^{+}) + \frac{1}{2}g^{2}s_{w}A_{\mu}\phi^{0}(W^{+}_{\mu}\phi^{-} + W^{-}_{\mu}\phi^{+}) + \frac{1}{2}g^{2}s_{w}A_{\mu}\phi^{0}(W^{+}_{\mu}\phi^{-} + W^{-}_{\mu}\phi^{+}) + \frac{1}{2}g^{2}s_{w}A_{\mu}\phi^{0}(W^{+}_{\mu}\phi^{-} + W^{-}_{\mu}\phi^{-}) + \frac{1}{2}g^{2}s_{w}A_{\mu}\phi^{0}(W^{+}_{\mu}\phi^{-}) + \frac{1}{2}g^{2}s_{w}A_{\mu}\phi^{0}(W^{+}_{\mu}$ $W^{\mu}_{\mu}\phi^{+}) + \frac{1}{2}ig^{2}s_{w}A_{\mu}H(W^{+}_{\mu}\phi^{-} - W^{-}_{\mu}\phi^{+}) - g^{2}\frac{s_{w}}{c_{w}}(2c_{w}^{2} - 1)Z^{0}_{\mu}A_{\mu}\phi^{+}\phi^{-} - g^{2}\frac{s_{w}}$ $g^{1}s_{w}^{2}A_{\mu}A_{\mu}\phi^{+}\phi^{-} - \bar{e}^{\lambda}(\gamma\partial + m_{e}^{\lambda})e^{\lambda} - \bar{\nu}^{\lambda}\gamma\partial\nu^{\bar{\lambda}} - \bar{u}_{i}^{\lambda}(\gamma\partial + m_{u}^{\lambda})u_{i}^{\lambda} \overset{j}{d_j} \overset{w}{(\gamma\partial} + m_d^{\lambda}) d_j^{\lambda} + igs_w A_{\mu} [-(\bar{e}^{\lambda} \gamma^{\mu} e^{\lambda}) + \frac{2}{3} (\bar{u}_j^{\lambda} \gamma^{\mu} u_j^{\lambda}) - \frac{1}{3} (\bar{d}_j^{\lambda} \gamma^{\mu} d_j^{\lambda})] +$ $\frac{ig}{4c_w}Z^0_{\mu}[(\bar{\nu}^{\lambda}\gamma^{\mu}(1+\gamma^5)\nu^{\lambda}) + (\bar{e}^{\lambda}\gamma^{\mu}(4s_w^2 - 1 - \gamma^5)e^{\lambda}) + (\bar{u}^{\lambda}_i\gamma^{\mu}(\frac{4}{3}s_w^2 - 1 - \gamma^5)e^{\lambda}) + (\bar{u}^{\lambda}_i\gamma^{\mu}(\frac{4}{3}s_w^2 - 1 - \gamma^5)e^{\lambda}) + (\bar{u}^{\lambda}_i\gamma^{\mu}(1+\gamma^5)\nu^{\lambda}) + (\bar{e}^{\lambda}\gamma^{\mu}(1+\gamma^5)\nu^{\lambda}) + (\bar{e}^{\lambda}\gamma^{\mu}(1+\gamma^5)\nu^{$ $1 - \gamma^{5} u_{j}^{\lambda} \right) + (\bar{d}_{j}^{\lambda} \gamma^{\mu} (1 - \frac{8}{3} s_{w}^{2} - \gamma^{5}) d_{j}^{\lambda})] + \frac{ig}{2\sqrt{2}} W_{\mu}^{+} [(\bar{\nu}^{\lambda} \gamma^{\mu} (1 + \gamma^{5}) \delta^{\lambda}) + (\bar{\nu}^{\lambda} \gamma^{\mu} (1 + \gamma^{5}) \delta^{\lambda})] + (\bar{\nu}^{\lambda} \gamma^{\mu} (1 - \gamma^{5}) \delta^{\lambda})] + (\bar{\nu}^{\lambda} \gamma^{\mu} (1 - \gamma^{5}) \delta^{\lambda}) + (\bar{\nu}^{\lambda} \gamma^{\mu} (1 - \gamma^{5}) \delta^{\lambda})] + (\bar{\nu}^{\lambda} \gamma^{\mu} (1 - \gamma^{5}) \delta^{\lambda}) + (\bar{\nu}^{\lambda} \gamma^{\mu} (1 - \gamma^{5}) \delta^{\lambda})] + (\bar{\nu}^{\lambda} \gamma^{\mu} (1 - \gamma^{5}) \delta^{\lambda}) + ($ $(\bar{u}_j^{\lambda}\gamma^{\mu}(1+\gamma^5)C_{\lambda\kappa}d_j^{\kappa})] + \frac{ig}{2\sqrt{2}}W^-_{\mu}[(\bar{e}^{\lambda}\gamma^{\mu}(1+\gamma^5)\nu^{\lambda}) + (\bar{d}_j^{\kappa}C_{\lambda\kappa}^{\dagger}\gamma^{\mu}(1+\gamma^5)\nu^{\lambda})]$ $(\gamma^5)u_j^{\lambda})] + \frac{ig}{2\sqrt{2}}\frac{m_{\lambda}^2}{M}[-\phi^+(\bar{\nu}^{\lambda}(1-\gamma^5)e^{\lambda}) + \phi^-(\bar{e}^{\lambda}(1+\gamma^5)\nu^{\lambda})] - \phi^+(\bar{\nu}^{\lambda}(1-\gamma^5)e^{\lambda}) + \phi^-(\bar{e}^{\lambda}(1-\gamma^5)\nu^{\lambda})]$ $\frac{q}{2}\frac{m_{\star}^{\lambda}}{M}[H(\bar{e}^{\lambda}e^{\lambda})+i\phi^{0}(\bar{e}^{\lambda}\gamma^{5}e^{\lambda})]+\frac{iq}{2M\sqrt{2}}\phi^{+}[-m_{d}^{\kappa}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1-\gamma^{5})d_{j}^{\kappa})+$ $m_u^{\lambda}(\bar{u}_j^{\lambda}C_{\lambda\kappa}(1+\gamma^5)d_j^{\kappa}] + \frac{ig}{2M\sqrt{2}}\phi^{-}[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa}) - m_u^{\kappa}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1-\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}}\phi^{-}[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa}) - m_u^{\kappa}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1-\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}}\phi^{-}[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa}) - m_u^{\kappa}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}}\phi^{-}[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa}) - m_u^{\kappa}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\prime}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}}\phi^{-}[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}}\phi^{-}[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}}\phi^{-}[m_d^{\lambda}(1+\gamma^5)u_j^{\kappa}) - \frac{ig}{2M\sqrt{2}}\phi^{-}[m_d^{\lambda}(1+\gamma^5)u_j^{\kappa}] + \frac{ig}{2M\sqrt{2}}\phi^{-}[m_d^{\lambda}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}}\phi^{-}[m_d^{\lambda}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}$ $\gamma^5 u_j^\kappa = -\frac{q}{2} \frac{m_u^\lambda}{M} H(\bar{u}_j^\lambda u_j^\lambda) - \frac{q}{2} \frac{m_d^\lambda}{M} H(\bar{d}_j^\lambda d_j^\lambda) + \frac{iq}{2} \frac{m_u^\lambda}{M} \phi^0(\bar{u}_j^\lambda \gamma^5 u_j^\lambda) - \frac{m_d^\lambda}{M} \phi^0(\bar{u}_j^\lambda \gamma^5 u_j^\lambda) - \frac{m_$ $\frac{ig}{2}\frac{m_d^\lambda}{M}\phi^0(\bar{d}_j^\lambda\gamma^5d_j^\lambda)+\bar{X}^+(\partial^2-M^2)X^++\bar{X}^-(\partial^2-M^2)X^-+\bar{X}^0(\partial$ $\frac{M^2}{c_*^2}$ $X^0 + \bar{Y}\partial^2 Y + igc_w W^+_\mu (\partial_\mu \bar{X}^0 X^- - \partial_\mu \bar{X}^+ X^0) + igs_w W^+_\mu (\partial_\mu \bar{Y} X^- - \partial_\mu \bar{X}^+ X^0)$ $\partial_{\mu}\bar{X}^{+}Y) + igc_{w}W^{-}_{\mu}(\partial_{\mu}\bar{X}^{-}X^{0} - \partial_{\mu}\bar{X}^{0}X^{+}) + igs_{w}W^{-}_{\mu}(\partial_{\mu}\bar{X}^{-}Y - \partial_{\mu}\bar{X}^{0}X^{+}))$ $\partial_{\mu}\bar{Y}X^{+}) + igc_{w}Z^{0}_{\mu}(\partial_{\mu}\bar{X}^{+}X^{+} - \partial_{\mu}\bar{X}^{-}X^{-}) + igs_{w}A_{\mu}(\partial_{\mu}\bar{X}^{+}X^{+} - \partial_{\mu}\bar{X}^{-}X^{-}) + igs_{w}A_{\mu}(\partial_{\mu}\bar{X}^{+}X^{+}) + igs_{w}A_{\mu}(\partial_{\mu}\bar{$ $\partial_{\mu}\bar{X}^{-}X^{-}) - \frac{1}{2}gM[\bar{X}^{+}X^{+}H + \bar{X}^{-}X^{-}H + \frac{1}{c^{2}}\bar{X}^{0}X^{0}H] +$ $\tfrac{1-2c_w^2}{2c_w}igM[\bar{X}^+X^0\phi^+-\bar{X}^-X^0\phi^-]+\tfrac{1}{2c_w}igM[\bar{X}^0X^-\phi^+-\bar{X}^0X^+\phi^-]+$ $igMs_w[\bar{X}^0X^-\phi^+ - \bar{X}^0X^+\phi^-] + \frac{1}{2}igM[\bar{X}^+X^+\phi^0 - \bar{X}^-X^-\phi^0]$

 $\pm m^{\lambda} e^{\lambda}$ $(\bar{e}^{\lambda}\gamma^{\mu}e^{\lambda}$ $(\bar{e}^{\lambda}\gamma^{\mu})$ $- \sim^5 \lambda d^{\lambda}$ $\frac{8}{2}$ 2





- Mercifully, there is a recipe for writing down that Lagrangian.
- Write down all terms that are:
- 1) Consistent with the symmetries of nature

Gauge invariance: $SU(3) \times SU(2)_L \times U(1)_Y$ + Lorentz invariance

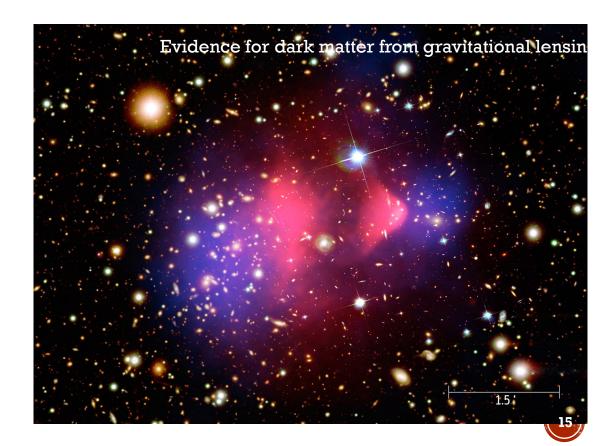
• 2) Renormalizible

All appear in nature, except 1 mystery absentee (strong CPV).



IS THERE MORE?

- We've never seen a particle interaction not predicted by the SM. But we suspect there is new physics out there...
 - Dark matter
 - Hierarchy problem
 - Gauge unification
 - Etc...
- Lots of ideas:
 - SUSY
 - Extra dimensions
 - String theory
 - Lorentz violation
 - [your favorite theory]



- We believe that whatever the new physics is, it kicks in a high energies (that's why we build accelerators).
- Technically we say the SM is likely a "low energy effective theory".

At high energies:

COMPLETE THEORY, VALID AT ALL ENERGIES



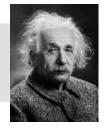
 $SU(3) \times SU(2)_L \times U(1)_Y$



• As a point of reference, here is another low energy effective theory:

At high energies:

$$E = \sqrt{p^2 + m^2}$$





$$E \sim m + p^2/2m$$



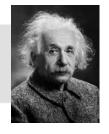


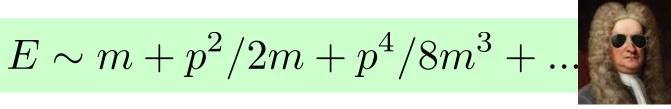
• As a point of reference, here is another low energy effective theory:

At high energies:

At low energies:

$$E = \sqrt{p^2 + m^2}$$



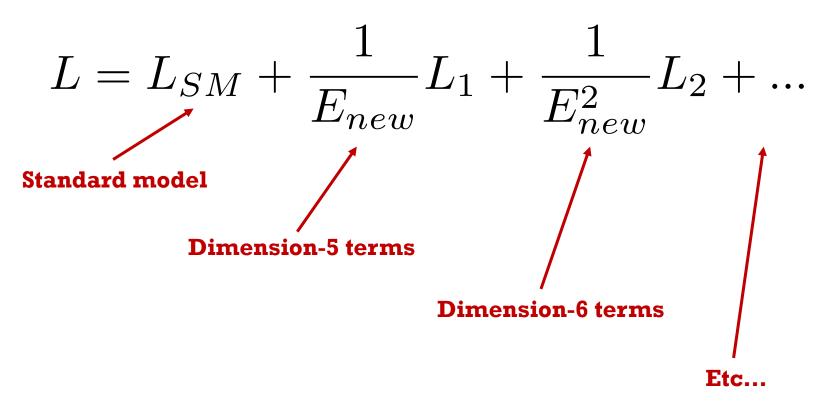


"dimension-4 correction"



And, we can test the high energy theory by confirming these corrections.

If SM is a low energy effective theory:



$$\begin{split} \mathbf{E}_{\mathrm{new}} &> 10 \, \mathrm{TeV} \\ \mathbf{E}_{\mathrm{new}} &\sim 10^{13} \, \mathrm{TeV} \\ \mathrm{scale}) \end{split}$$

Seems likely (LHC) Maybe? (GUT



If SM is a low energy effective theory:

$$L = L_{SM} + \frac{1}{E_{new}}L_1 + \frac{1}{E_{new}^2}L_2 + \dots$$

 The only dimension-5 operator one can add obeying SM gauge symmetry:

$$\frac{L_1}{E_{new}} = y_{ij} \frac{\nu^i H \nu^j H}{E_{new}}$$
Weinberg 1979.

- This term does an important thing it makes neutrinos Majorana particles, with mass suppressed by the new physics scale.
- And it makes the theory non-renormalizible implying there must be something else at high scale.

DOUBLE-BETA DECAY

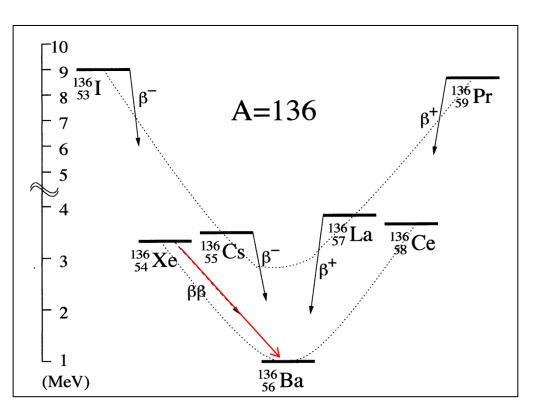
allowed *β*β

A rare radioactive process, energetically allowed for some even-even nuclei where $m_{Z+1} > m_Z > m_{Z+2}$

```
(Z,A) \rightarrow (Z+2,A) + e_1 + \underline{v}_1 + e_2 + \underline{v}_2
```

(NB: this decay mode has nothing to do with Majorana neutrinos, but we'll get back to them soon)







Direct Evidence for Two-Neutrino Double-Beta Decay in ⁸²Se

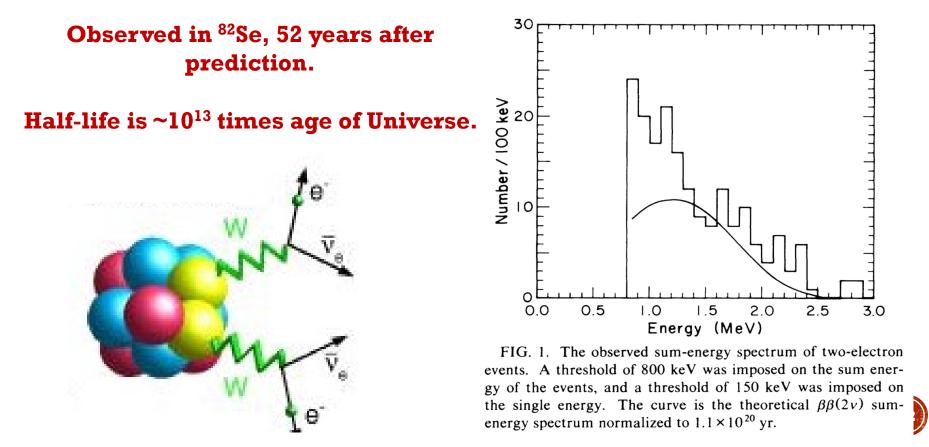
S. R. Elliott, A. A. Hahn, and M. K. Moe

Department of Physics, University of California, Irvine, Irvine, California 92717 (Received 31 August 1987)

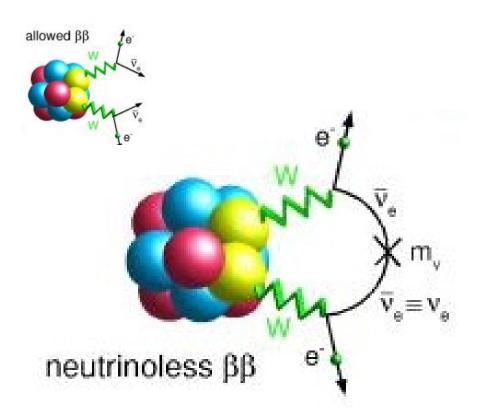
The two-neutrino mode of double-beta decay in ⁸²Se has been observed in a time-projection chamber at a half-life of $(1.1\pm0.3)\times10^{20}$ yr (68% confidence level). This result from direct counting confirms the earlier geochemical measurements and helps provide a standard by which to test the double-beta-decay matrix elements of nuclear theory. It is the rarest natural decay process ever observed directly in the laboratory.

PACS numbers: 23.40.Bw

Discovery of double beta decay



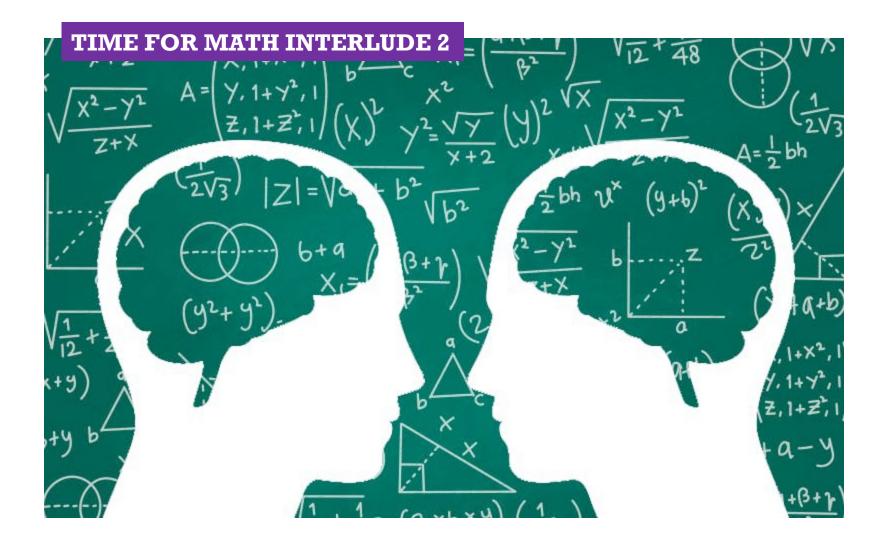
DOUBLE BETA WITH NO NEUTRINOS?



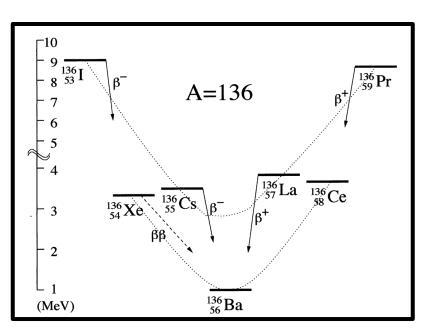
- This can only happen if the neutrino is its own antiparticle.
- Observation of double beta decay with no neutrinos would prove the neutrino to be a Majorana fermion.

How fast will this decay go? Lets find out!



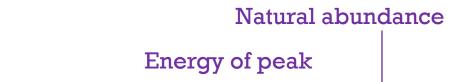






DOUBLE BETA ISOTOPES

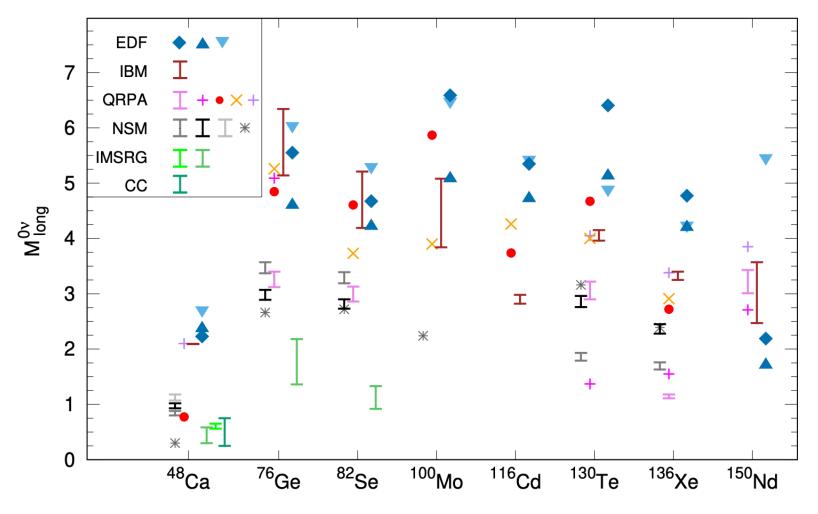
- Larger $G \rightarrow$ higher rate
- Helps if Q is above most background γ rays
- Abundance, cost, and ease of enrichment are also factors influencing isotope choice.



Phase space factor

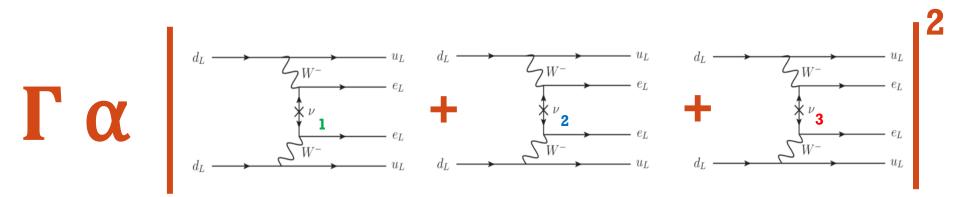
Isotope	$G^{0\nu}$	$Q_{\beta\beta}$	Nat. ab.
⁴⁸ Ca	$\frac{(10^{-14} \text{ y}^{-1})}{6.35}$	(keV)	$\frac{(\%)}{0.187}$
⁷⁶ Ge	0.55	4273.7 2039.1	7.8
⁸² Se		2039.1 2995.5	
^{Se} ⁹⁶ Zr	2.70		9.2
¹⁰⁰ Mo	5.63	3347.7	2.8
	4.36	3035.0	9.6
¹¹⁰ Pd	1.40	2004.0	11.8
¹¹⁶ Cd	4.62	2809.1	7.6
¹²⁴ Sn	2.55	2287.7	5.6
¹³⁰ Te	4.09	2530.3	34.5
¹³⁶ Xe	4.31	2461.9	8.9
¹⁵⁰ Nd	19.2	3367.3	5.6

NUCLEAR MATRIX ELEMENTS

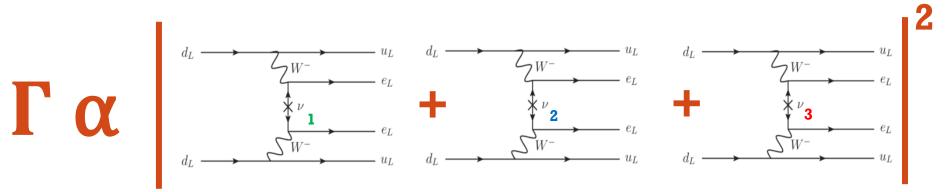


Agostini, Benato, Detwiler, JM, Vissani, Rev. Mod. Phys. 95, 025002 (2023)



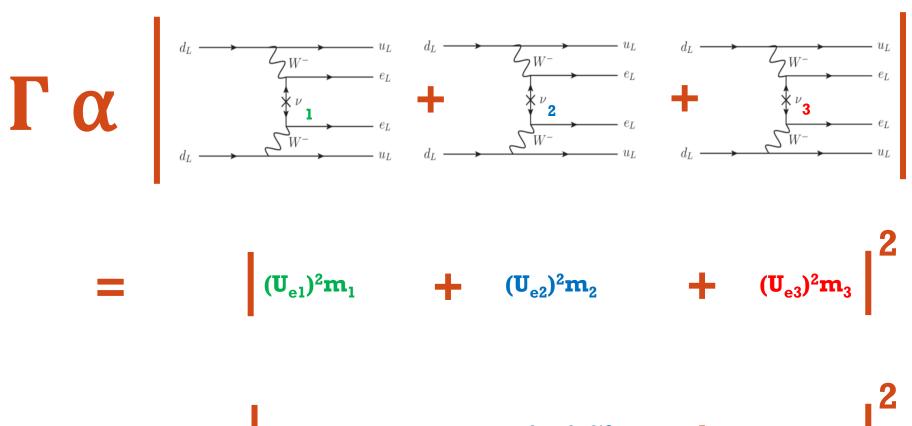






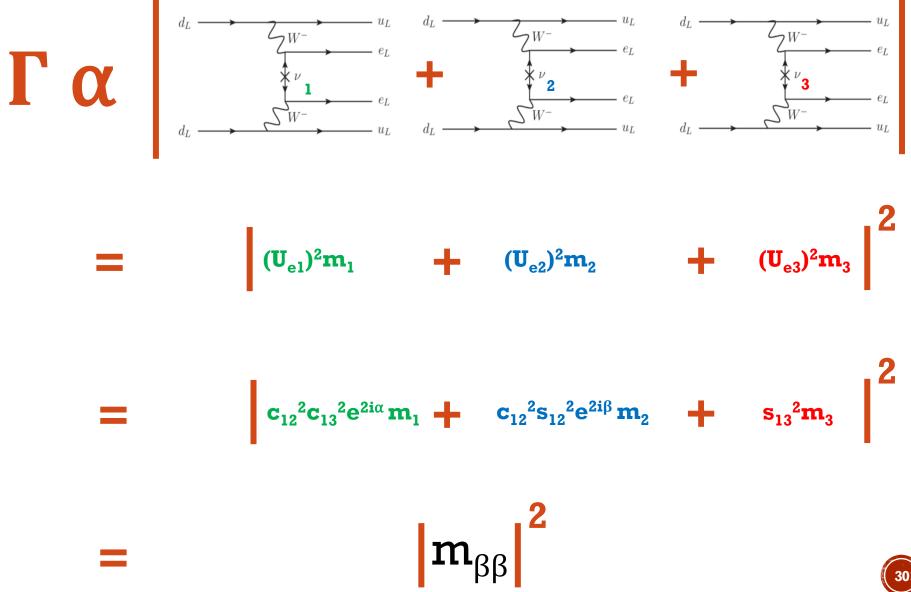




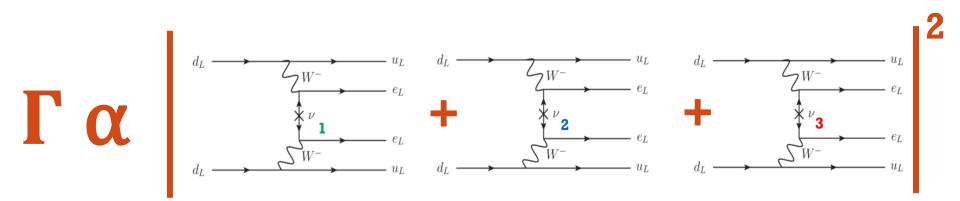


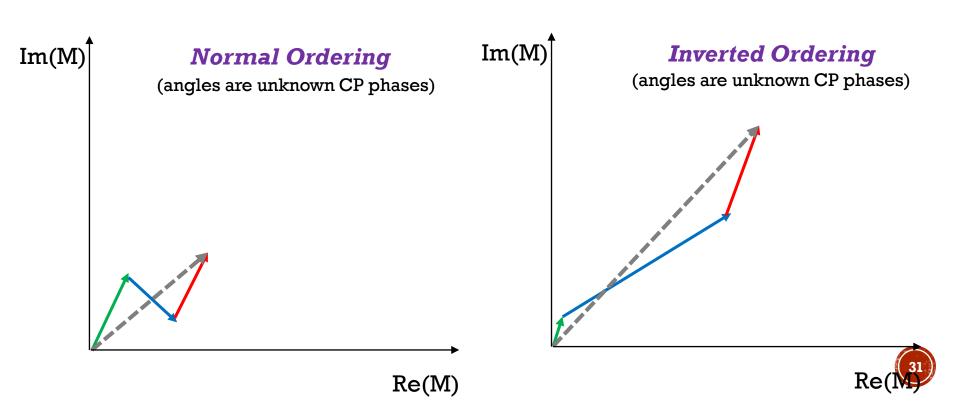
 $c_{12}^{\ 2}c_{13}^{\ 2}e^{2i\alpha}m_1 + c_{12}^{\ 2}s_{12}^{\ 2}e^{2i\beta}m_2 + s_{13}^{\ 2}m_3$

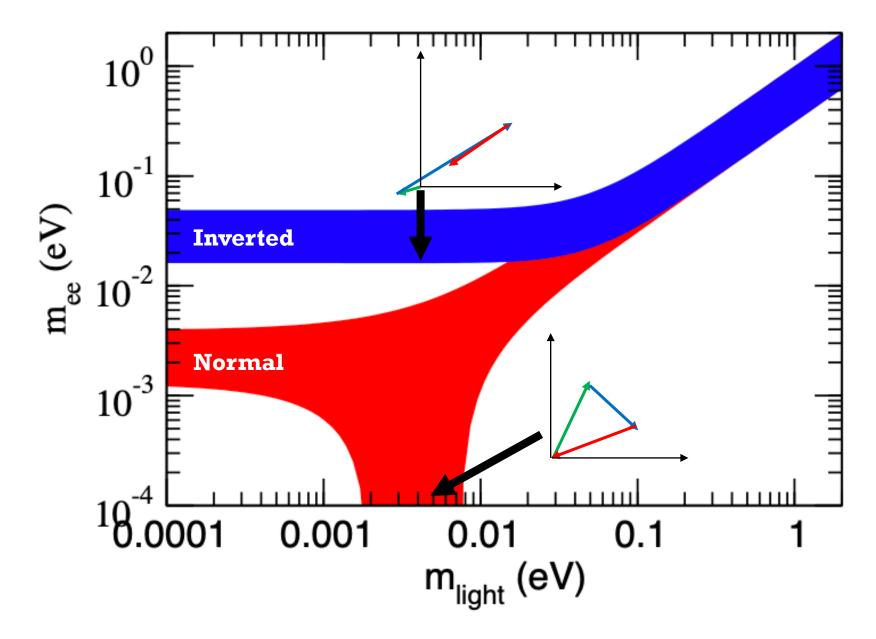




Ζ

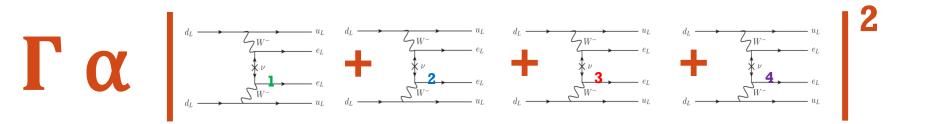


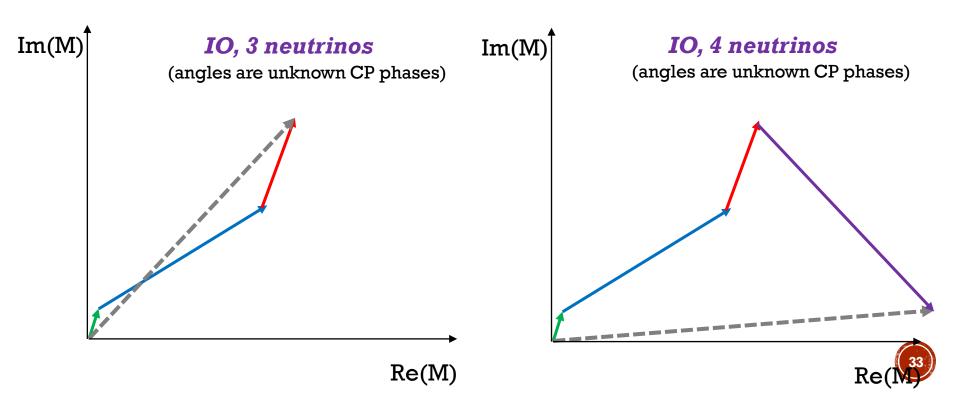




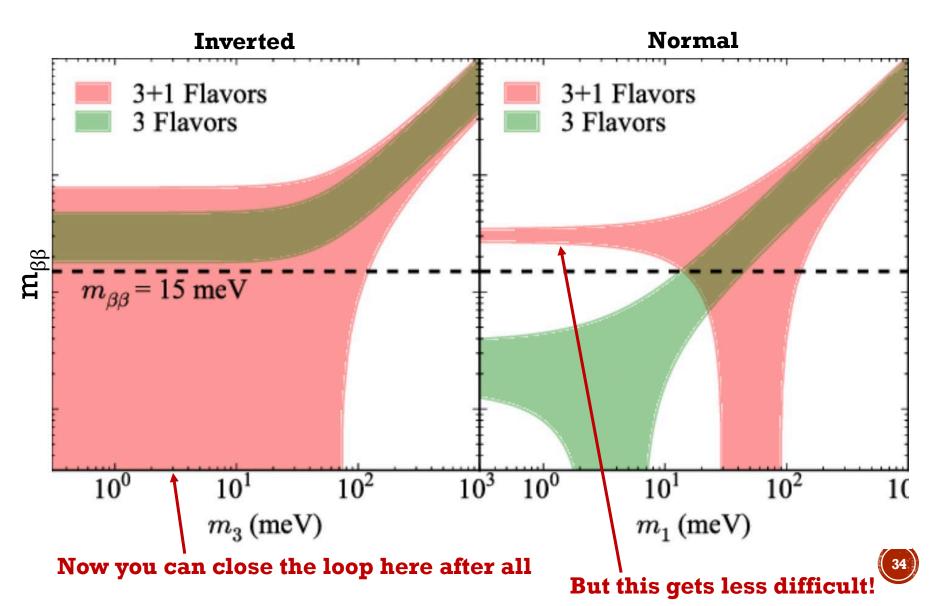


WHAT IF THERE ARE ADDITIONAL NEUTRINOS?

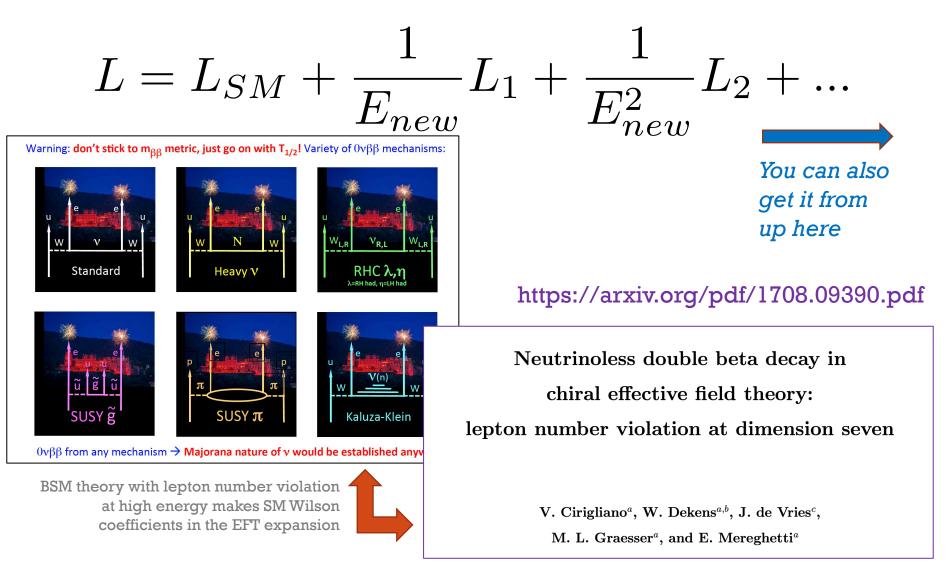




WITH A STERILE NEUTRINO:



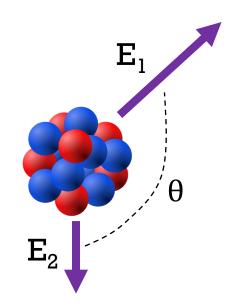
If SM is a low energy effective theory:

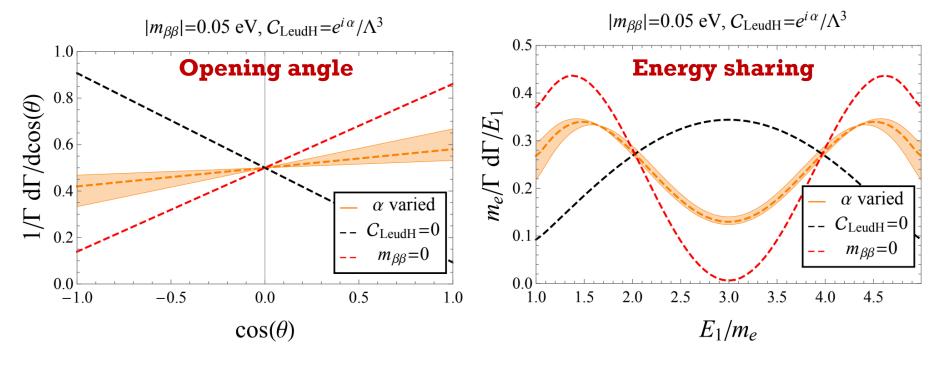


So really we need to consider 0nubb as a discovery search – just hit the longest half lives possible!



- Given a high energy model, the kinematics of the final electrons can be predicted.
- If 0nubb is seen, measuring the opening angle and energy sharing could illuminate the mechanism.

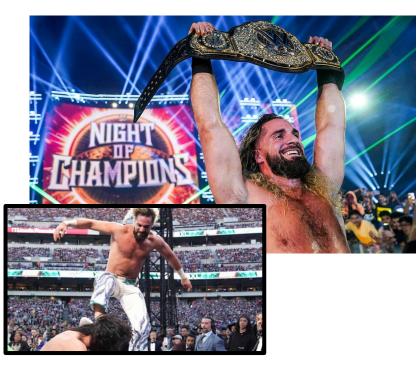




CURRENT WORLD HEAVYWEIGHT CHAMPION



WWE world heavyweight champion



Seth "Freakin" Rollins



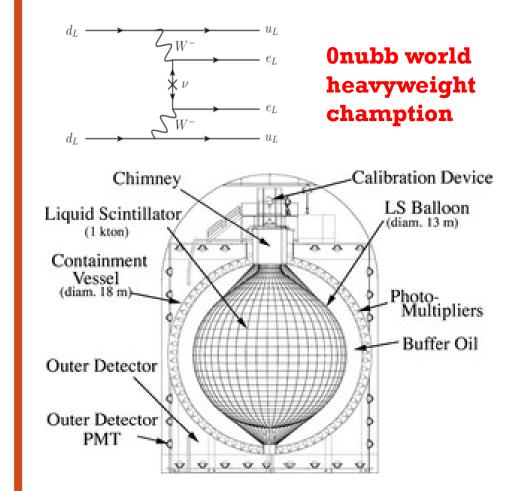
CURRENT WORLD HEAVYWEIGHT CHAMPION



WWE world heavyweight champion



Seth "Freakin" Rollins



Kamland "Freakin" Zen 38



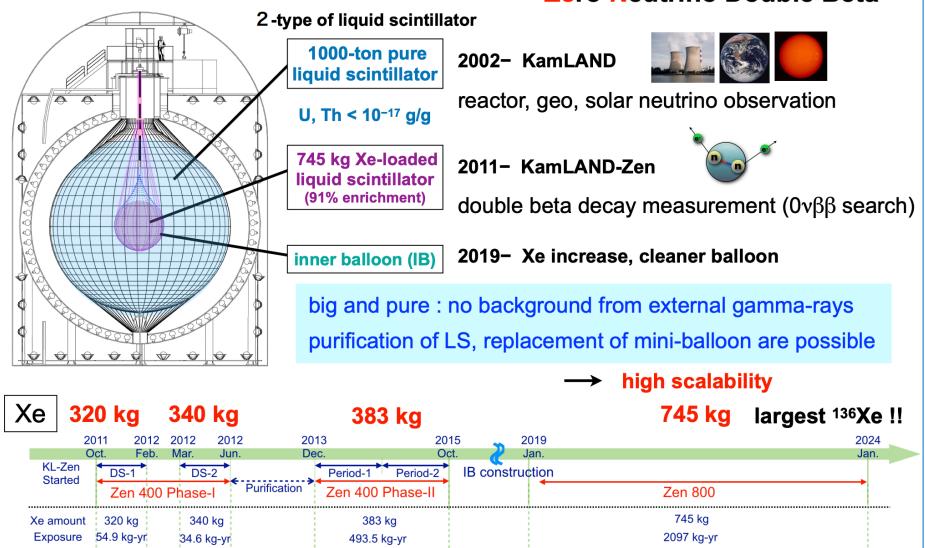
From Neutrino2024

Kamioka underground

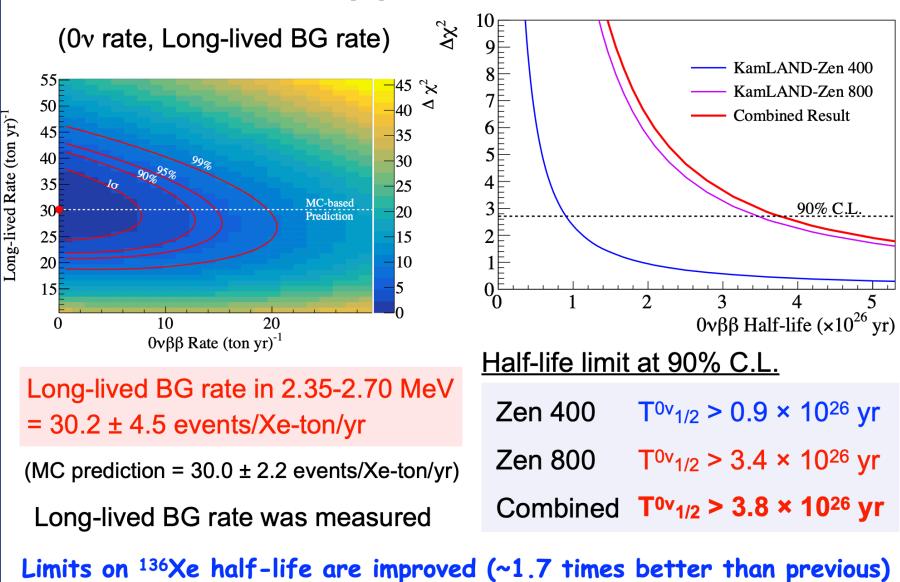
KamLAND detector

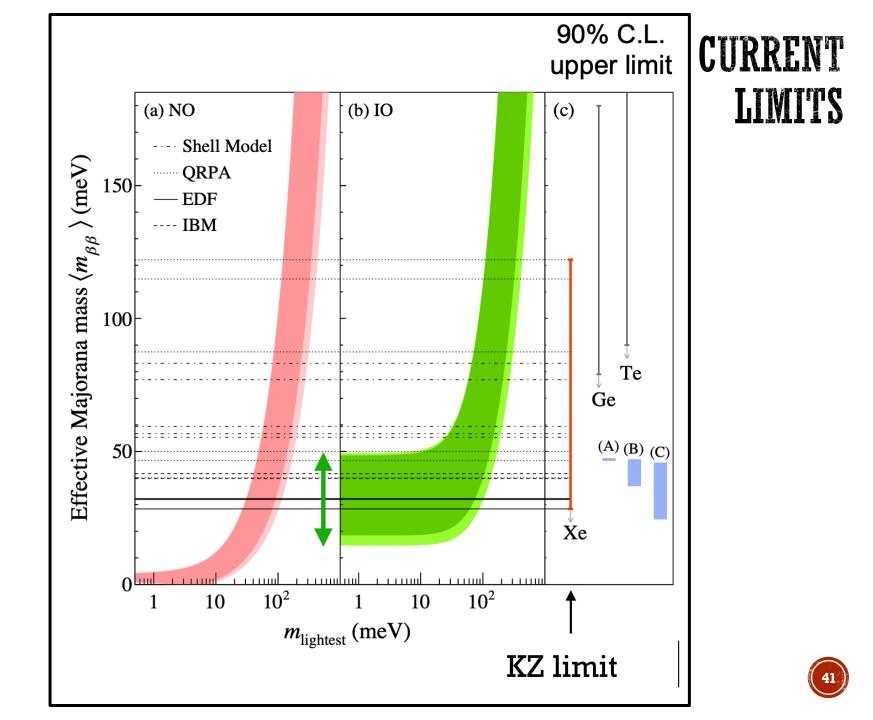
KamLAND-Zen

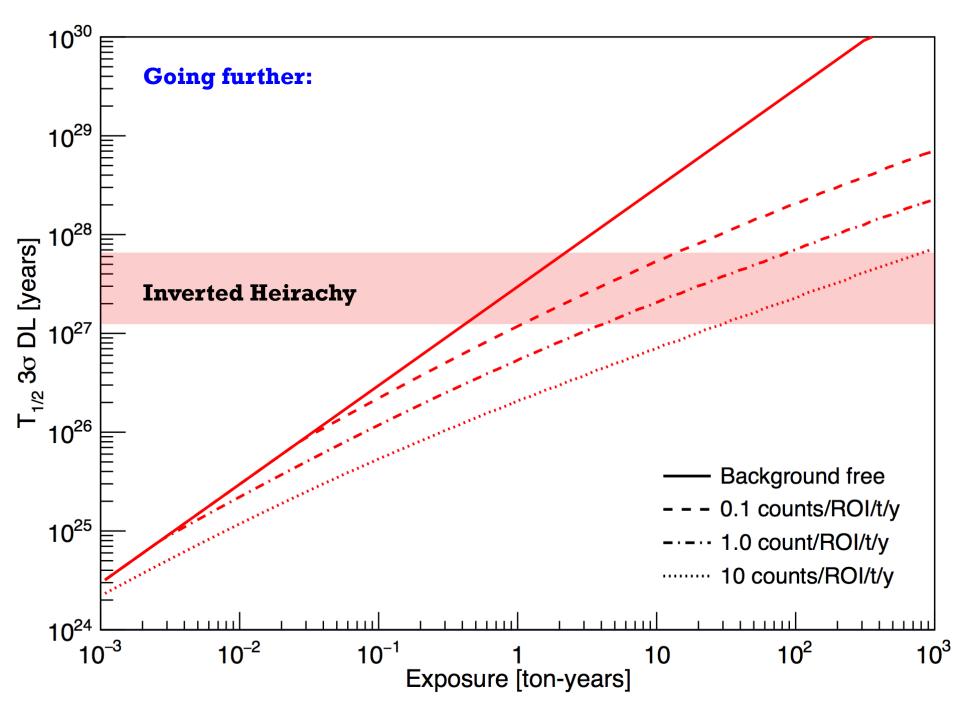
Zero Neutrino Double Beta

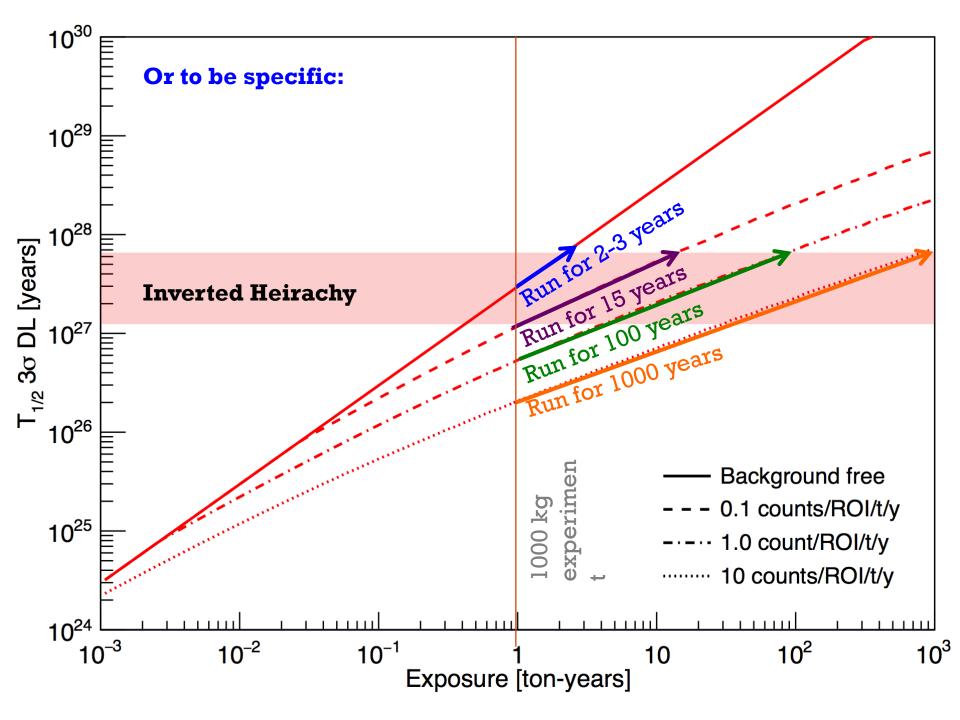


¹³⁶Xe $0\nu\beta\beta$ Decay Half-life









Where are the backgrounds from?

(nb: these are pre-Neutrino2024 numbers) TABLE I: Summary of the estimated and best-fit background contributions for the frequentist and Bayesian analyses in the energy region 2.35 < E < 2.70 MeV within the 1.57-m-radius spherical volume. In total, 24 events were observed.

Background	Estimated	Best-fit			
		Frequentist	Bayesian		
136 Xe $2 uetaeta$	-	11.98	11.95		
Residual radioactivity in Xe-LS					
²³⁸ U series	0.14 ± 0.04	0.14	0.09		
232 Th series	-	0.84	0.87		
External (Radioactivity in IB)					
²³⁸ U series	-	3.05	3.46		
²³² Th series	-	0.01	0.01		
Neutrino interactions					
⁸ B solar νe^{-1}	$\mathrm{ES} \qquad 1.65 \pm 0.04$	1.65	1.65		
Spallation products					
Long-lived	$7.75\pm0.57~^\dagger$	12.52	11.80		
$^{10}\mathrm{C}$	0.00 ± 0.05	0.00	0.00		
⁶ He	0.20 ± 0.13	0.22	0.21		
¹³⁷ Xe	0.33 ± 0.28	0.34	0.34		

[†] Estimation based on the spallation MC study. This event rate constraint is not applied to the spectrum fit.

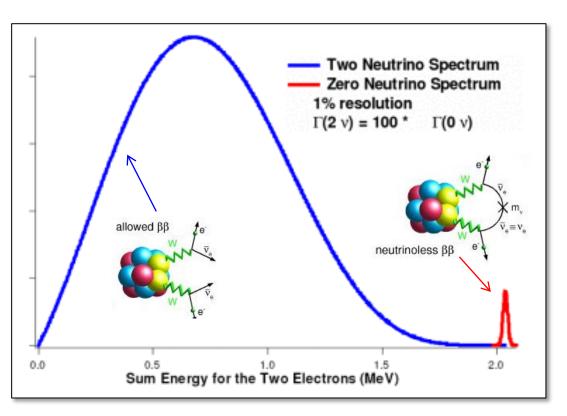
Where are the backgrounds from?

TABLE I: Summary of the estimated and best-fit background contributions for the frequentist and Bayesian analyses in the energy region 2.35 < E < 2.70 MeV within the 1.57-m-radius spherical volume. In total, 24 events were observed.

Background	Estimated	Best-fit			
		Frequentist	Bavesian		
136 Xe $2 uetaeta$	-	11.98	11.95		
Residual radioactivity in Xe-LS					
²³⁸ U series	0.14 ± 0.04	0.14	0.09		
232 Th series	-	0.84	0.87		
External (Radioactivity in IB)					
²³⁸ U series	-	3.05	3.46		
232 Th series	-	0.01	0.01		
Neutrino interactions					
⁸ B solar νe^{-1}	$\mathrm{ES} \qquad 1.65 \pm 0.04$	1.65	1.65		
Spallation products					
Long-lived	$7.75\pm0.57~^\dagger$	12.52	11.80		
$^{10}\mathrm{C}$	0.00 ± 0.05	0.00	0.00		
⁶ He	0.20 ± 0.13	0.22	0.21		
¹³⁷ Xe	0.33 ± 0.28	0.34	0.34		

[†] Estimation based on the spallation MC study. This event rate constraint is not applied to the spectrum fit.

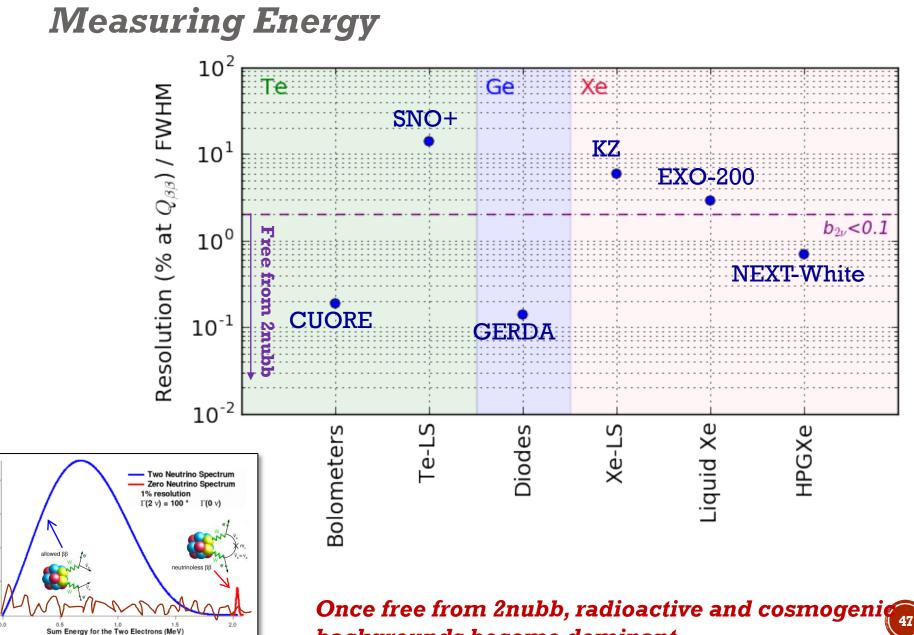
THE IDEAL EXPERIMENT:



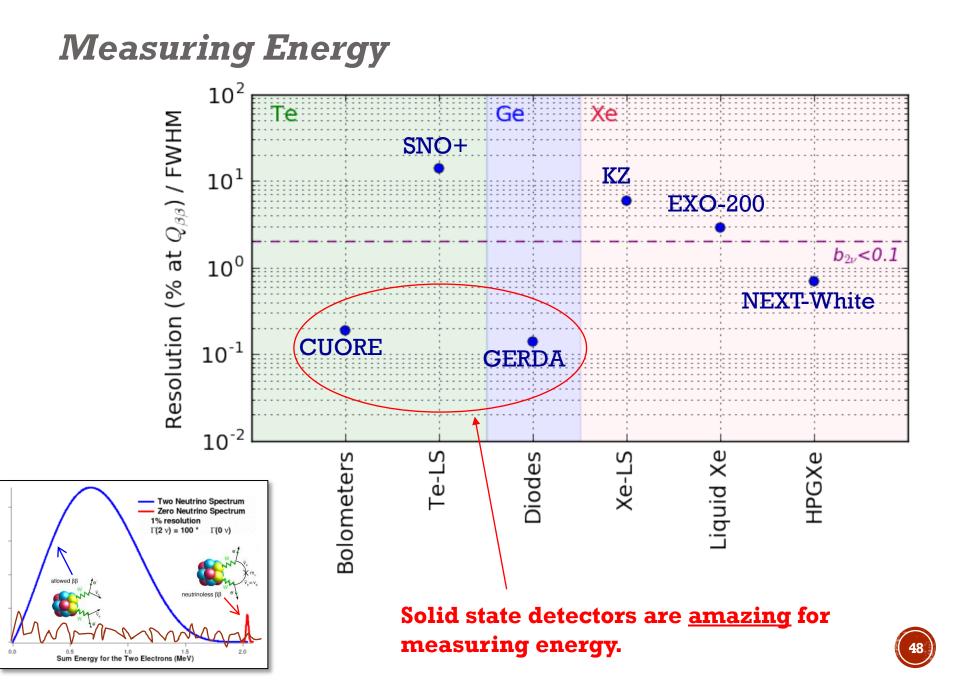
- MANDATORY:
 - Resolution better than ~2% FWHM to fully reject twoneutrino mode

Then just watch and wait...



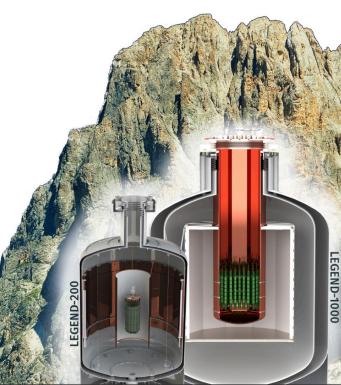


backgrounds become dominant

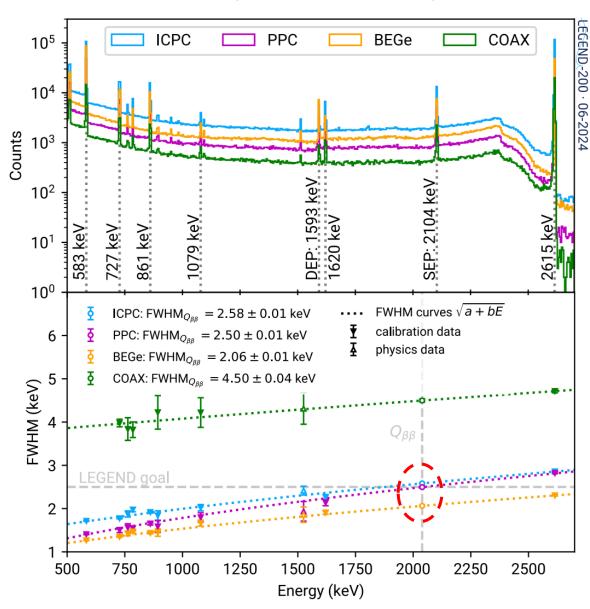


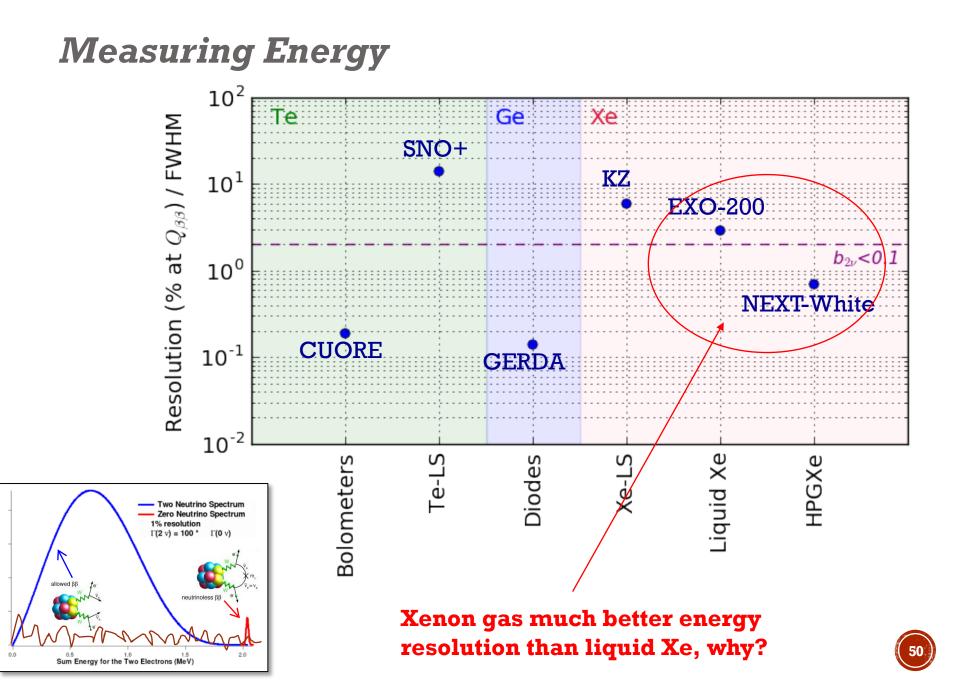
LEGEND

- 200kg, eventually 1000kg, of enriched ⁷⁶Ge crystals
- The king of excellent E resolution 0.1%FWHM in the best crystals.



LEGEND200 backgrounds and energy resolutions:





RECOMBINATION-LIMITED IONIZATION ENERGY RESOLUTION

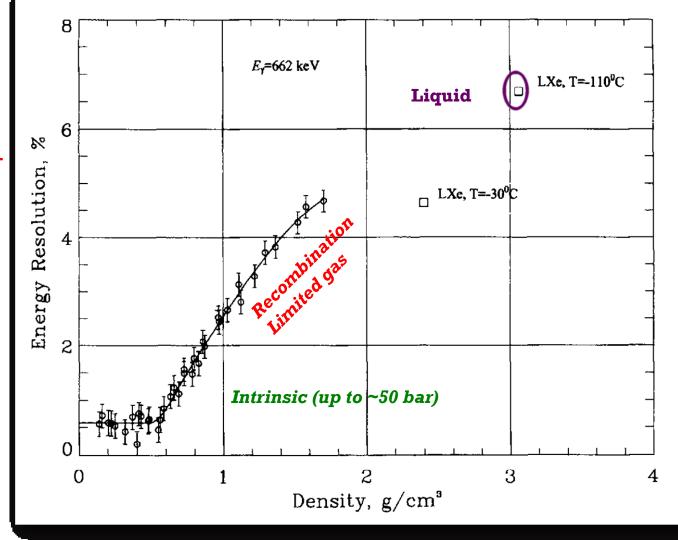
Fluctuations in electronion recombination limit energy resolution for dense TPCs.

e

e

e⁻

Every event is a random microscopic shape, so each loses different amounts of charge to recombination.





Where are the backgrounds from?

Radiogenics

Solar neutrinos(!)

Cosmogenics

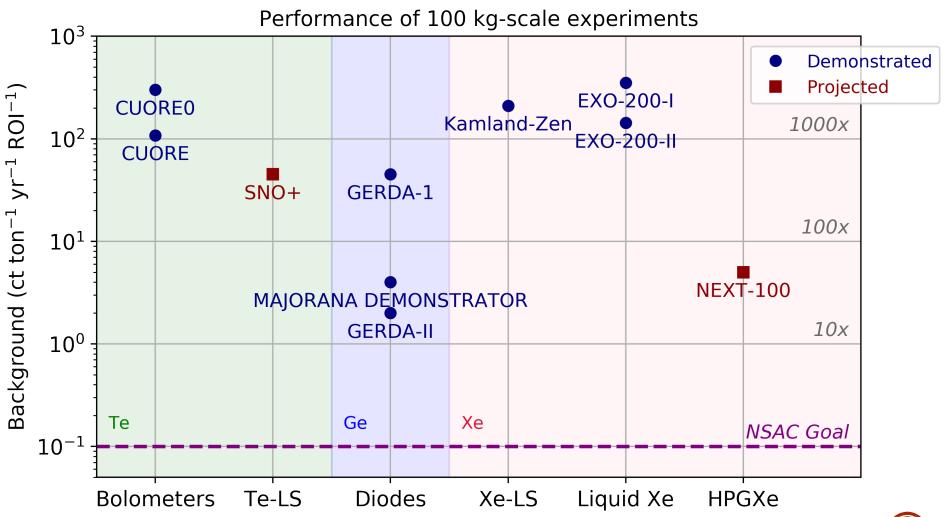
These will limit all future experiments.

TABLE I: Summary of the estimated and best-fit background contributions for the frequentist and Bayesian analyses in the energy region 2.35 < E < 2.70 MeV within the 1.57-m-radius spherical volume. In total, 24 events were observed.

Estimated	Best-fit				
	Frequentist	Bayesian			
-	11.98	11.95			
Residual radioactivity in Xe-LS					
0.14 ± 0.04	0.14	0.09			
-	0.84	0.87			
External (Radioactivity in IB)					
-	3.05	3.46			
-	0.01	0.01			
Neutrino interactions					
ES 1.65 ± 0.04	1.65	1.65			
Spallation products					
7.75 ± 0.57 $^{ op}$	12.52	11.80			
0.00 ± 0.05	0.00	0.00			
0.20 ± 0.13	0.22	0.21			
0.33 ± 0.28	0.34	0.34			
	Residual radioactivity 0.14 ± 0.04 - External (Radioactiv - Neutrino interac ES 1.65 \pm 0.04 Spallation prod 7.75 ± 0.57 + 0.00 ± 0.05 0.20 ± 0.13	Frequentist - 11.98 Residual radioactivity in Xe-LS 0.14 \pm 0.04 0.14 - 0.84 External (Radioactivity in IB) - Spallation interactivity Residual radioactivity in IB) -			

[†] Estimation based on the spallation MC study. This event rate constraint is not applied to the spectrum fit.

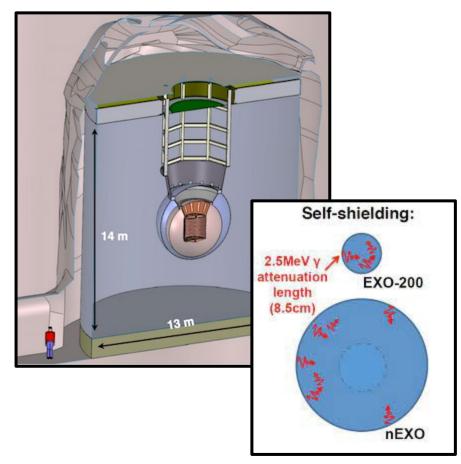
"100kg-class" experiments:



53

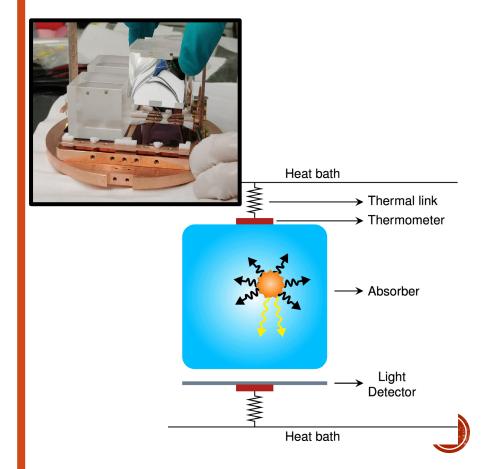
NEX0

- Proposed ton-scale liquid xenon detector.
- Self-shielding of xenon from outer regions protects inner clean volume from backgrounds

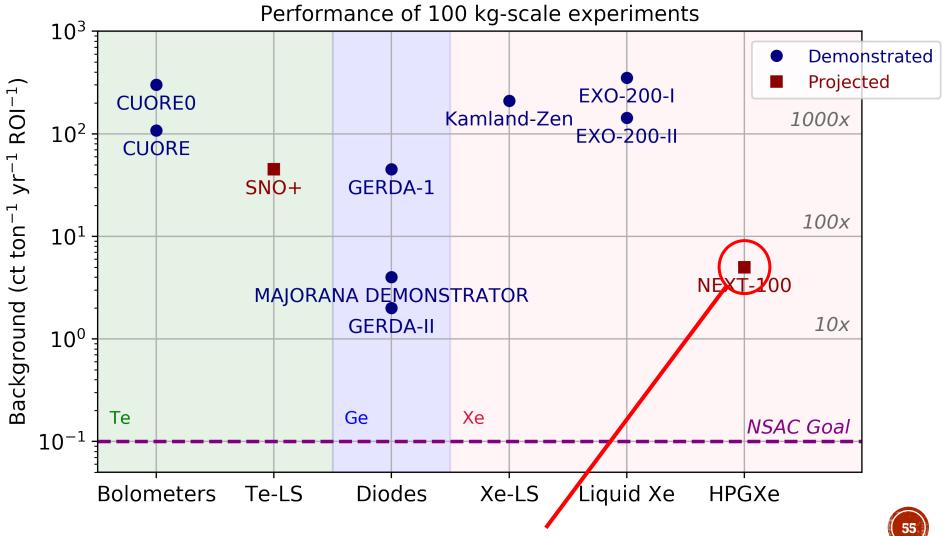


CUPID

- Cryogenic bolometers coupled to light sensors
- Precise calorimetry and optical handle on surface backgrounds advances on the CUORE approach.



"100kg-class" experiments:

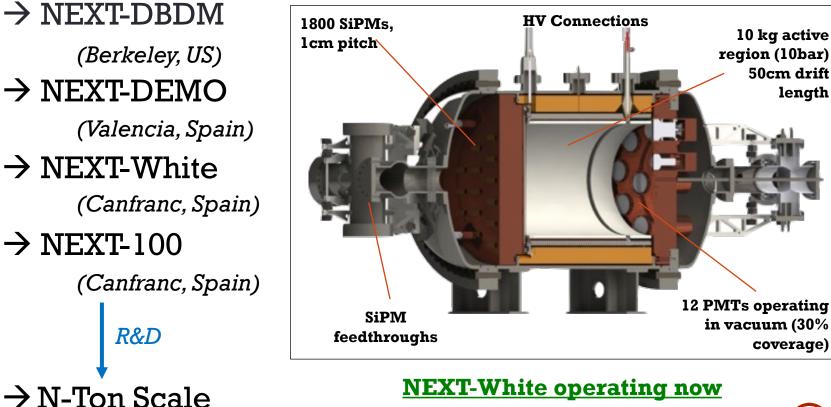


I work on this one, so I'm going to tell you about it.

THE NEXT PROGRAM

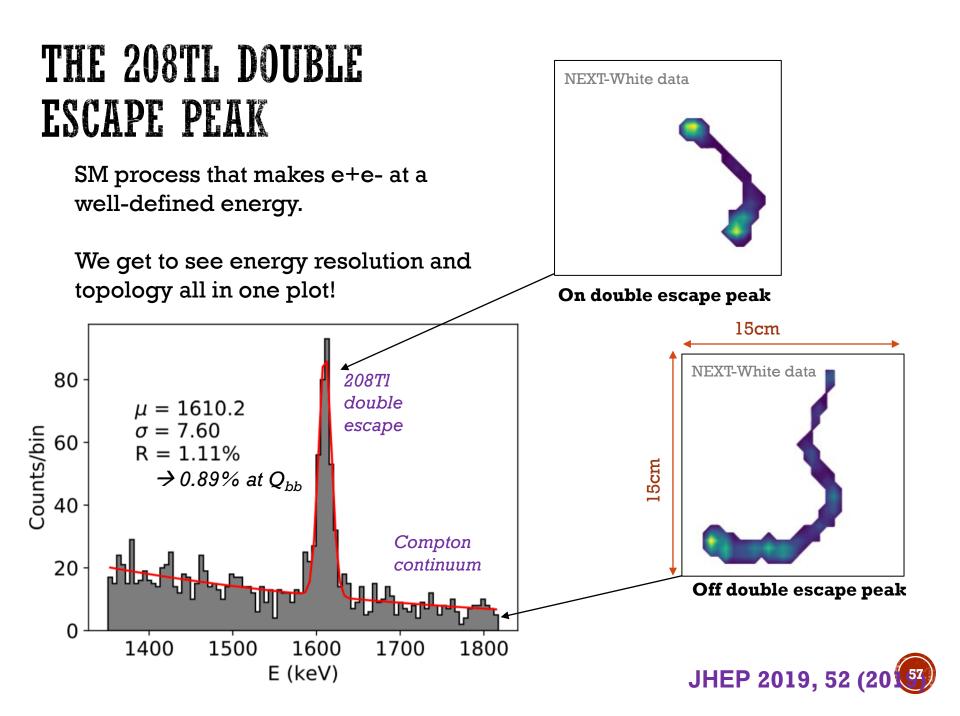


- Sequence of HPGXe TPCs, focused on achieving big, very low background xenon $0\nu\beta\beta$ detector

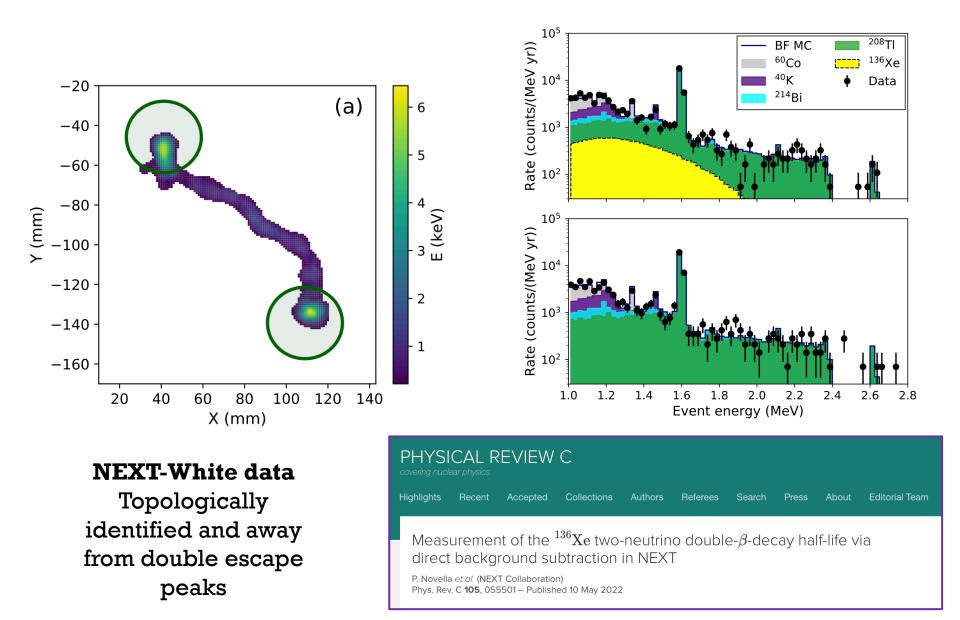


Full underground technology demonstrator @10kg scale





TWO-NEUTRINO DOUBLE BETA DECAY EVENTS

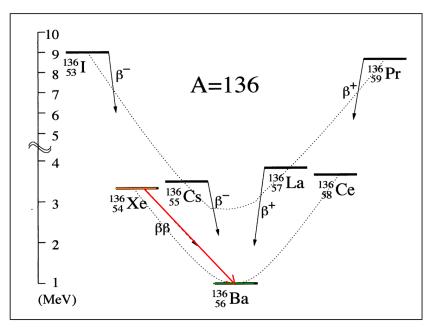


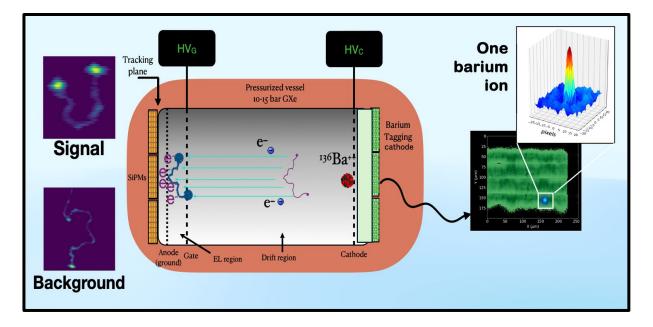
BARIUM TAGGING

(My fave thing: forgive me for indulging \bigcirc)

Barium ion is only produced in a true $\beta\beta$ decay, not in any other radioactive event \rightarrow

Identification of Ba ion plus $\sim 1\%$ FWHM energy measurement would give a background-free experiment. 136 Xe \rightarrow 136 Ba + e + e





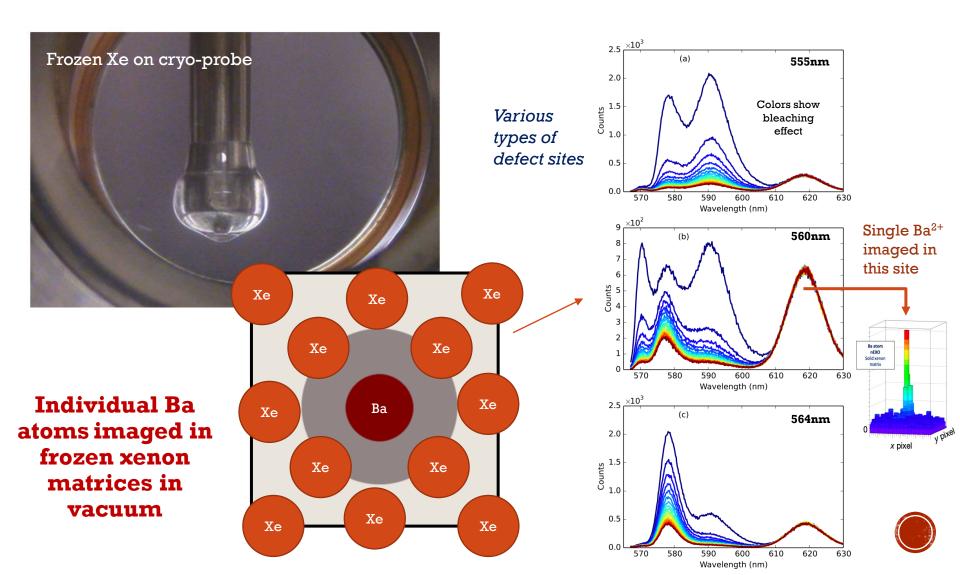
Is it plausible to detect an individual barium ion or atom in a ton of material, inside a working xenon TPC?



BA IMAGING IN XENON ICE



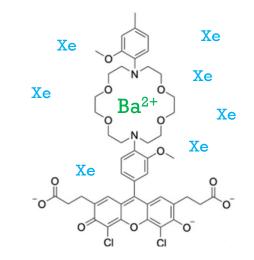
nEXO has developed methods of imaging Ba^+ and Ba^0 in carefully grown xenon ice.

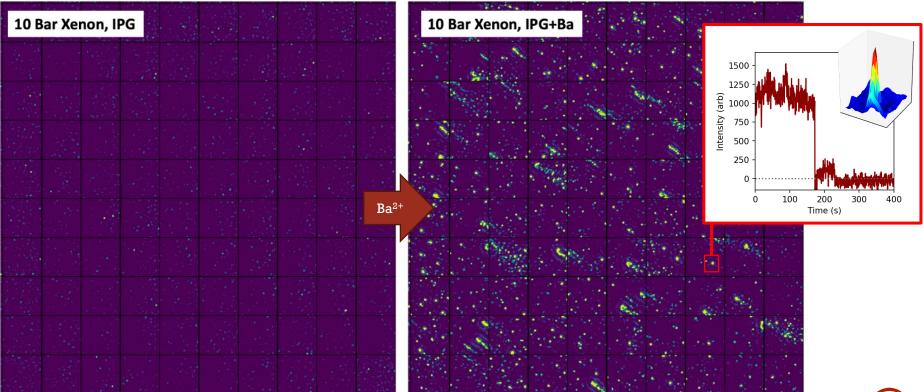


BA IMAGING IN XENON GAS

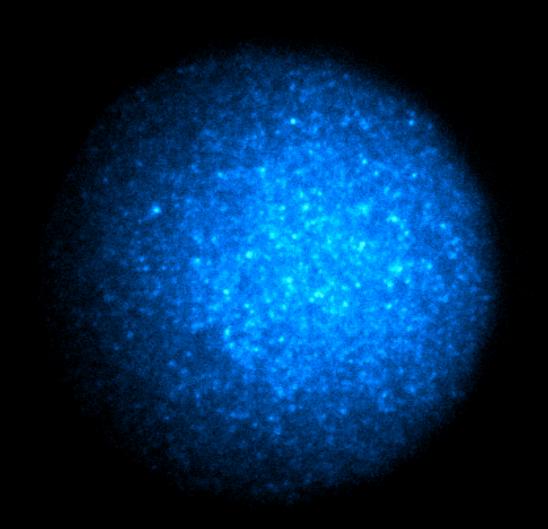
NEXT has built microscopy systems capable of imaging individual barium ions in high pressure xenon gas environments.

1mm x 1mm area can be scanned with single ion precision.



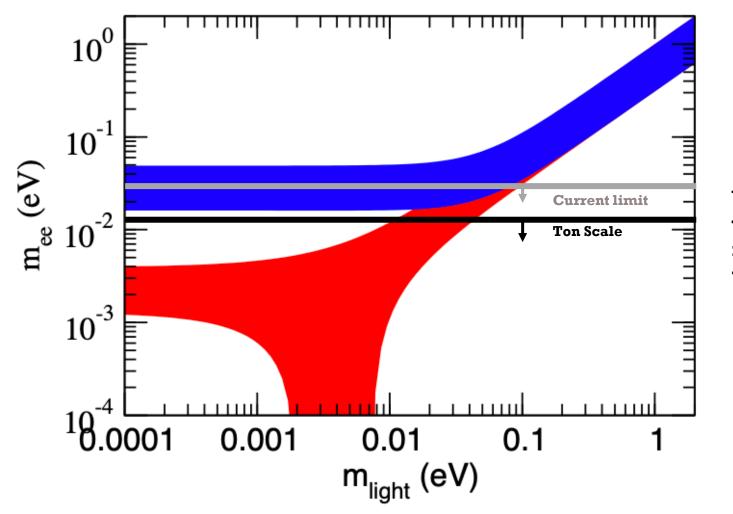






Single Ba²⁺ molecular complexes

THE TON SCALE

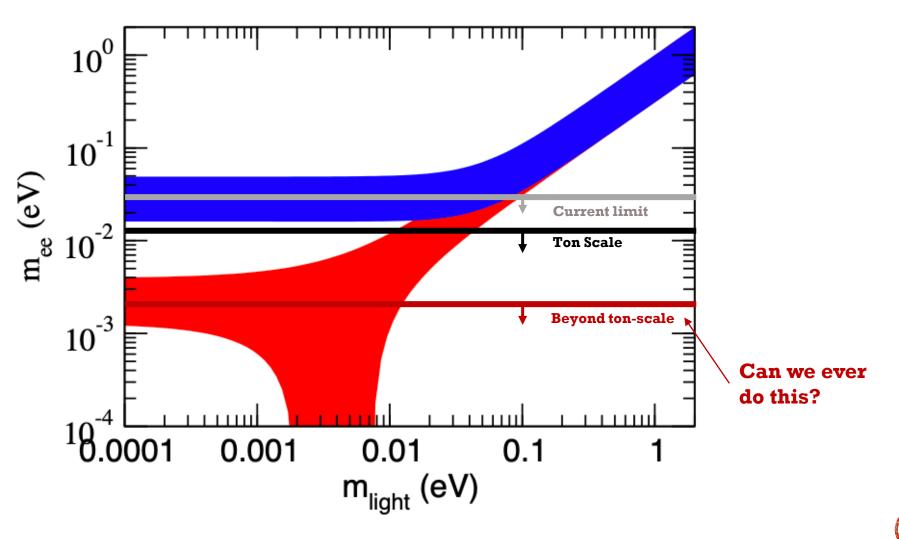


We need to do this with multiple isotopes and techniques



NB: if you use these tons, the sensitivity will be better.

TOWARD NORMAL ORDERING



65

ISOTOPES

- Will need hundreds of tons of isotope. Current industrial production of any species is insufficient.
- There are difficulties with both acquisition of raw material and its enrichment.
- Some notable factoids:
 - Tellurium:

Comes naturally enriched to 34%. So natural tellurium is the most viable for an unenriched experiment.

Molybdenum:

New capacity for enrichment of Molybdenum in 100Mo for nuclear medicine is needed. 0nubb may be parasitic?

• Germanium:

Semiconductor industry enriches germanium already; 76Ge can in principle be extracted as byproduct?

Xenon:

Atmospheric carbon capture technology based on metal organic frameworks has plausible extendibility to capture atmospheric Xe. Free from steel industry capacity limit?

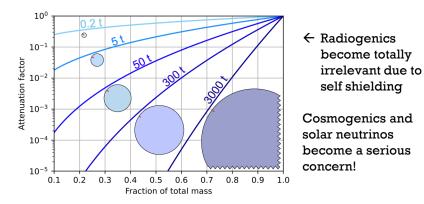
 Both enrichment R&D and new major facilities would be needed to produce isotope at the scale needed for a normalordering scale experiment.



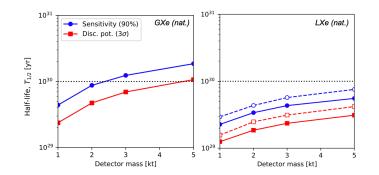
GIANT TPCS

Kiloton-scale xenon detectors for neutrinoless double beta decay and other new physics searches

A. Avasthi,¹ T.W. Bowyer,² C. Bray,³ T. Brunner,^{4,5} N. Catarineu,⁶ E. Church,² R. Guenette,⁷
S.J. Haselschwardt,⁸ J.C. Hayes,² M. Heffner,^{6,*} S.A. Hertel,⁹ P.H. Humble,² A. Jamil,¹⁰ S.H. Kim,⁶
R.F. Lang,¹¹ K.G. Leach,³ B.G. Lenardo,¹² W.H. Lippincott,¹³ A. Marino,³ D.N. McKinsey,^{14, 8}
E.H. Miller,^{15, 16} D.C. Moore,^{10, †} B. Mong,¹⁵ B. Monreal,¹ M.E. Monzani,^{15, 16} I. Olcina,^{8, 14} J.L. Orrell,²
S. Pang,⁶ A. Pocar,⁹ P.C. Rowson,¹⁵ R. Saldanha,² S. Sangiorgio,⁶ C. Stanford,⁷ and A. Visser⁶



If energy resolution achievable at scale, with kiloton masses, normal ordering parameter space is accessible.

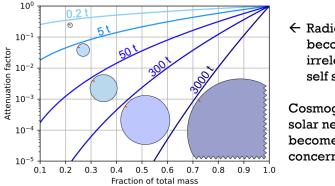




GIANT TPCS

Kiloton-scale xenon detectors for neutrinoless double beta decay and other new physics searches

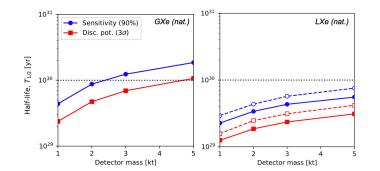
A. Avasthi,¹ T.W. Bowyer,² C. Bray,³ T. Brunner,^{4,5} N. Catarineu,⁶ E. Church,² R. Guenette,⁷
S.J. Haselschwardt,⁸ J.C. Hayes,² M. Heffner,^{6,*} S.A. Hertel,⁹ P.H. Humble,² A. Jamil,¹⁰ S.H. Kim,⁶
R.F. Lang,¹¹ K.G. Leach,³ B.G. Lenardo,¹² W.H. Lippincott,¹³ A. Marino,³ D.N. McKinsey,^{14,8}
E.H. Miller,^{15,16} D.C. Moore,^{10,†} B. Mong,¹⁵ B. Monreal,¹ M.E. Monzani,^{15,16} I. Olcina,^{8,14} J.L. Orrell,²
S. Pang,⁶ A. Pocar,⁹ P.C. Rowson,¹⁵ R. Saldanha,² S. Sangiorgio,⁶ C. Stanford,⁷ and A. Visser⁶



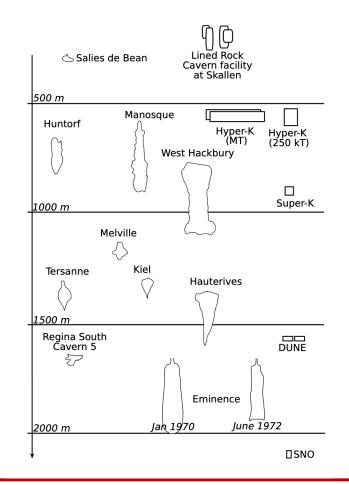
← Radiogenics become totally irrelevant due to self shielding

Cosmogenics and solar neutrinos become a serious concern!

If energy resolution achievable at scale, with kiloton masses, normal ordering parameter space is accessible.



... in salt caverns?



High-pressure TPCs in pressurized caverns: opportunities in dark matter and neutrino physics

Author:

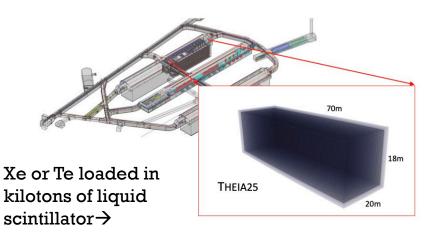
Benjamin Monreal (Case Western Reserve U.) [benjamin.monreal@case.edu]

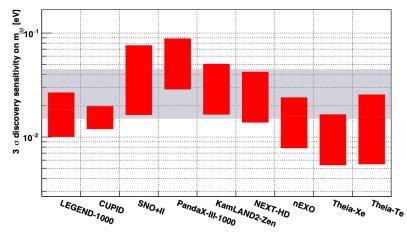
ISOTOPE IN KTONS OF LIQUID SCINTILLATOR...

THEIA: Summary of physics program

Snowmass White Paper Submission

M. Askins,^{1,2} Z. Bagdasarian,^{1,2} N. Barros,^{3,4,5} E.W. Beier,³ A. Bernstein,⁶ M. Böhles,⁷ E. Blucher,⁸





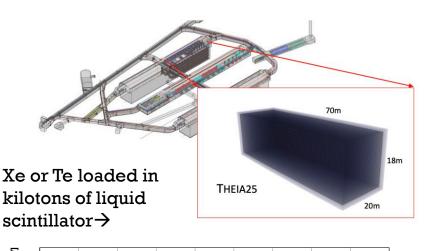


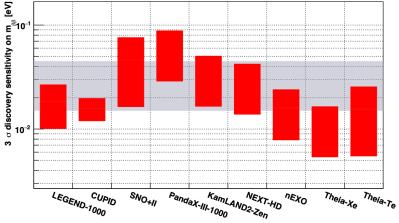
ISOTOPE IN KTONS OF LIQUID SCINTILLATOR...

THEIA: Summary of physics program

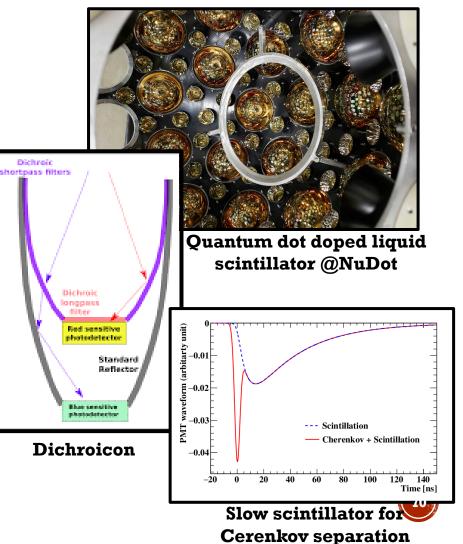
Snowmass White Paper Submission

M. Askins,^{1,2} Z. Bagdasarian,^{1,2} N. Barros,^{3,4,5} E.W. Beier,³ A. Bernstein,⁶ M. Böhles,⁷ E. Blucher,⁸

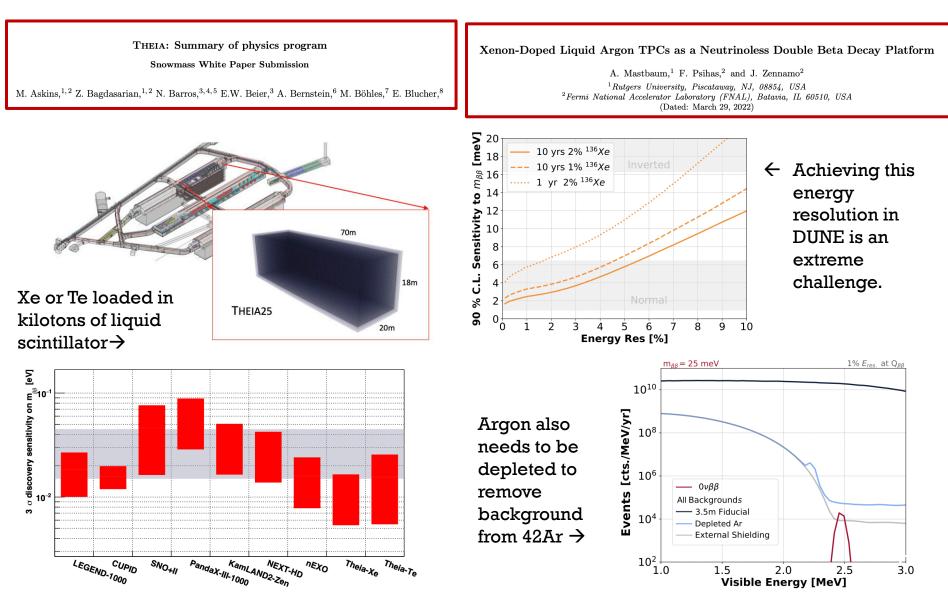




Much, much R&D...



ISOTOPE IN KTONS LS, OR IN LIQUID ARGON?



CONCLUSIONS

- NDBD is the only sensitive known way to probe the Majorana nature of the neutrino.
- Experiments at the 100kg scale have demonstrated background indices in the range 2-200 ct/ton/ky/yr
- Ton-scale experiments plan to reduce backgrounds by 1.5-3 orders of magnitude relative 100kg phases and probe the inverted mass ordering range of parameter space.
- Beyond-ton-scale will require huge, ultra-low background detectors that we don't yet know how to build, but need to figure out!

